### Monetary Policy According to HANK

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#### HANK: Heterogeneous Agent New Keynesian models

 Framework for quantitative analysis of the transmission mechanism of monetary policy



#### HANK: Heterogeneous Agent New Keynesian models

- Framework for quantitative analysis of the transmission mechanism of monetary policy
- Three building blocks
  - 1. Uninsurable idiosyncratic income risk
  - 2. Nominal price rigidities
  - 3. Assets with different degrees of liquidity



# How monetary policy works in RANK

• Total consumption response to a drop in real rates

$$C \text{ response} = \underbrace{\text{direct response to } r}_{>95\%} + \underbrace{\text{indirect effects due to } Y}_{<5\%}$$

• Direct response is everything, pure intertemporal substitution



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- Direct response is everything, pure intertemporal substitution
- However, data suggest:
  - 1. Low sensitivity of C to r
  - 2. Sizable sensitivity of C to Y
  - 3. Micro sensitivity vastly heterogeneous, depends crucially on household balance sheets



# How monetary policy works in HANK

- Once matched to micro data, HANK delivers realistic:
  - Wealth distribution: small direct effect
  - MPC distribution: large indirect effect (depending on  $\Delta Y$ )



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• Overall effect depends crucially on fiscal response, unlike in RANK where Ricardian equivalence holds



# Outline

#### 1. Model

#### 2. Parameterization

#### 3. Results

#### 4. Additional Material

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# Households

- Face uninsured idiosyncratic labor income risk
- Consume and supply labor
- Hold two assets: liquid and illiquid



# Households

- Face uninsured idiosyncratic labor income risk
- Consume and supply labor
- Hold two assets: liquid and illiquid
- Budget constraints (simplified version)

$$\dot{b_t} = r^b b_t + w z_t \ell_t - c_t - d_t - \chi(d_t, a_t)$$
  
$$\dot{a_t} = r^a a_t + d_t$$

- $b_t$ : liquid assets
- a<sub>t</sub>: illiquid assets
- $d_t$ : illiquid deposits ( $\geq 0$ )  $\chi$ : transaction cost function
- In equilibrium:  $r^a > r^b$
- Full model: borrowing/saving rate wedge, taxes/transfers



# Kinked adjustment cost function $\chi(d, a)$





# **Remaining model ingredients**

Illiquid assets: a = k + qs

• No arbitrage:  $r^k - \delta = \frac{\Pi + \dot{q}}{q} := r^a$ 

#### Firms

- Monopolistic intermediate-good producers  $\rightarrow$  final good
- Rent capital and labor services
- Quadratic price adjustment costs à la Rotemberg (1982)

#### Government

• Issues liquid debt  $(B^g)$ , spends (G), taxes and transfers (T)

#### Monetary Authority

• Sets nominal rate on liquid assets based on a Taylor rule



### Summary of market clearing conditions

• Liquid asset market

 $B^h + B^g = 0$ 

• Illiquid asset market

$$A = K + q$$

Labor market

$$N=\int z\ell(a,b,z)d\mu$$

• Goods market:

 $Y = C + I + G + \chi + \Theta$  + borrowing costs



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  - Liquid (cash, bank accounts + government/corporate bonds)
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  - Match mean liquid/illiquid wealth and fraction HtM
  - Production side: standard calibration of NK models
  - Separable preferences:  $u(c, \ell) = \log c \frac{1}{2}\ell^2$



### Model matches key feature of U.S. wealth distribution





# Model generates high and heterogeneous MPCs





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Innovation  $\epsilon < 0$  to the Taylor rule:  $i = \bar{r}^b + \phi \pi + \epsilon$ 

• All experiments:  $\epsilon_0 = -0.0025$ , i.e. -1% annualized



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$$dC_{0} = \underbrace{\int_{0}^{\infty} \frac{\partial C_{0}}{\partial r_{t}^{b}} dr_{t}^{b} dt}_{\text{direct}} + \underbrace{\int_{0}^{\infty} \left[ \frac{\partial C_{0}}{\partial r_{t}^{a}} dr_{t}^{a} + \frac{\partial C_{0}}{\partial w_{t}} dw_{t} + \frac{\partial C_{0}}{\partial T_{t}} dT_{t} \right] dt}_{\text{indirect}}$$



$$dC_{0} = \int_{0}^{\infty} \frac{\partial C_{0}}{\partial r_{t}^{b}} dr_{t}^{b} dt + \int_{0}^{\infty} \left[ \frac{\partial C_{0}}{\partial r_{t}^{a}} dr_{t}^{a} + \frac{\partial C_{0}}{\partial w_{t}} dw_{t} + \frac{\partial C_{0}}{\partial T_{t}} dT_{t} \right] dt$$

$$\checkmark$$

Intertemporal substitution and income effects from  $r^b \downarrow$ 





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$$\checkmark$$

Portfolio reallocation effect from  $r^a - r^b \uparrow$ 





$$dC_{0} = \int_{0}^{\infty} \frac{\partial C_{0}}{\partial r_{t}^{b}} dr_{t}^{b} dt + \int_{0}^{\infty} \left[ \frac{\partial C_{0}}{\partial r_{t}^{a}} dr_{t}^{a} + \frac{\partial C_{0}}{\partial w_{t}} dw_{t} + \frac{\partial C_{0}}{\partial T_{t}} dT_{t} \right] dt$$

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Labor demand channel from  $w \uparrow$ 





$$dC_{0} = \int_{0}^{\infty} \frac{\partial C_{0}}{\partial r_{t}^{b}} dr_{t}^{b} dt + \int_{0}^{\infty} \left[ \frac{\partial C_{0}}{\partial r_{t}^{a}} dr_{t}^{a} + \frac{\partial C_{0}}{\partial w_{t}} dw_{t} + \frac{\partial C_{0}}{\partial T_{t}} dT_{t} \right] dt$$

Fiscal adjustment:  $T \uparrow$  in response to  $\downarrow$  in interest payments on B





$$dC_{0} = \underbrace{\int_{0}^{\infty} \frac{\partial C_{0}}{\partial r_{t}^{b}} dr_{t}^{b} dt}_{19\%} + \underbrace{\int_{0}^{\infty} \left[ \frac{\partial C_{0}}{\partial r_{t}^{a}} dr_{t}^{a} + \frac{\partial C_{0}}{\partial w_{t}} dw_{t} + \frac{\partial C_{0}}{\partial T_{t}} dT_{t} \right] dt}_{81\%}$$





#### Monetary transmission across liquid wealth distribution



• Total change = c-weighted sum at each liquid wealth level b



# Why small direct effects?



- Income effect: (-) for rich households
- Intertemporal substitution: (+) for non-HtM
- Portfolio reallocation: (-) for those with low but > 0 liquid wealth



### Fiscal response important for total effect

	T adjusts	G adjusts	B <sup>g</sup> adjusts
	(1)	(2)	(3)
Elasticity of $Y_0$ to $r^b$	-3.96	-7.74	-2.17
Elasticity of $C_0$ to $r^b$	-2.93	-2.80	-1.68
Share of Direct effects:	19%	21%	42%

- Fiscal response to lower interest payments on debt:
  - T adjusts: stimulates AD through MPC of HtM households
  - G adjusts: translates 1-1 into AD
  - B<sup>g</sup> adjusts: no initial stimulus to AD from fiscal side



### Comparison to one-asset HANK model





### When is HANK $\neq$ RANK? Persistence

• RANK: 
$$\frac{\dot{C}_t}{C_t} = \frac{1}{\gamma}(r_t - \rho) \Rightarrow C_0 = \bar{C} \exp\left(-\frac{1}{\gamma}\int_0^\infty (r_s - \rho)ds\right)$$

- Cumulative *r*-deviation  $R_0 := \int_0^\infty (r_s \rho) ds$  is sufficient statistic
- Persistence  $\eta$  only matters insofar as it affects  $R_0$

$$-rac{d\log C_0}{dR_0}=rac{1}{\gamma}=1 \quad ext{for all } \eta$$



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### Inflation-output tradeoff same as in RANK





#### Monetary transmission in RANK and HANK

 $\Delta C = \text{direct response to } r + \text{indirect GE response} \\ \text{RANK: 95\%} \\ \text{HANK: 1/3} \\ \text{HANK: 2/3}$ 



# Monetary transmission in RANK and HANK

 $\Delta C = \text{direct response to } r + \text{indirect GE response} \\ \text{RANK: 95\%} \\ \text{HANK: 1/3} \\ \text{HANK: 2/3}$ 

- RANK view:
  - High sensitivity of C to r: intertemporal substitution
  - Low sensitivity of C to Y: the RA is a PIH consumer
- HANK view:
  - Low sensitivity to *r*: income effect of wealthy offsets int. subst.
  - High sensitivity to *Y*: sizable share of hand-to-mouth agents

 $\Rightarrow$  **Q:** Is Fed less in control of *C* than we thought?



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# Literature and contribution

Combine two workhorses of modern macroeconomics:

- New Keynesian models Gali, Gertler, Woodford
- Bewley models Aiyagari, Bewley, Huggett



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#### Closest existing work:

New Keynesian models with limited heterogeneity

Campell-Mankiw, Gali-LopezSalido-Valles, Jacoviello, Bilbiie, Challe-Matheron-Ragot-Rubio-Ramirez

micro-foundation of spender-saver behavior

#### Bewley models with sticky prices

Oh-Reis, Guerrieri-Lorenzoni, Bavn-Sterk, Gornemann-Kuester-Nakaiima, DenHaan-Rendal-Rieoler, Baver-Luetticke-Pham-Tiaden, McKav-Reis,

McKay-Nakamura-Steinsson, Huo-RiosRull, Werning, Luetticke

- assets with different liquidity Kaplan-Violante
- new view of individual earnings risk Guvenen-Karahan-Ozkan-Song
- Continuous time approach Achdou-Han-Lasry-Lions-Moll CHICAGO

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#### Households

$$\max_{\{c_t, \ell_t, d_t\}_{t \ge 0}} \mathbb{E}_0 \int_0^\infty e^{-(\rho+\lambda)t} u(c_t, \ell_t) dt \quad \text{s.t.}$$
  
$$\dot{b}_t = r^b(b_t) b_t + w z_t \ell_t - d_t - \chi(d_t, a_t) - c_t - \tilde{T} (w z_t \ell_t + \Gamma) + \Gamma$$
  
$$\dot{a}_t = r^a a_t + d_t$$
  
$$z_t = \text{some Markov process}$$
  
$$b_t \ge -\underline{b}, \quad a_t \ge 0$$

- $c_t$ : non-durable consumption
- *b<sub>t</sub>*: liquid assets
- $z_t$ : individual productivity
- $\ell_t$ : hours worked
- *a<sub>t</sub>*: illiquid assets

- $d_t$ : illiquid deposits ( $\geq 0$ )
- $\chi$ : transaction cost function
- $\tilde{T}$ : income tax/transfer
- Γ: income from firm ownership
- no housing see working paper

#### Households

• Adjustment cost function

$$\chi(d, a) = \chi_0 |d| + \chi_1 \left| \frac{d}{\max\{a, \underline{a}\}} \right|^{\chi_2} \max\{a, \underline{a}\}$$

- Linear component implies inaction region
- · Convex component implies finite deposit rates





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- Linear component implies inaction region
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- Recursive solution of hh problem consists of:
  - 1. consumption policy function  $c(a, b, z; w, r^a, r^b)$
  - 2. deposit policy function  $d(a, b, z; w, r^a, r^b)$
  - 3. labor supply policy function  $\ell(a, b, z; w, r^a, r^b)$
  - $\Rightarrow$  joint distribution of households  $\mu(da, db, dz; w, r^a, r^b)$



#### **Firms**

Representative competitive final goods producer:

$$Y = \left(\int_0^1 y_j^{\frac{\varepsilon-1}{\varepsilon}} dj\right)^{\frac{\varepsilon}{\varepsilon-1}} \quad \Rightarrow \quad y_j = \left(\frac{p_j}{P}\right)^{-\varepsilon} Y$$



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Monopolistically competitive intermediate goods producers:

- Technology:  $y_j = Z k_j^{\alpha} n_j^{1-\alpha} \quad \Rightarrow \quad m = \frac{1}{Z} \left(\frac{r}{\alpha}\right)^{\alpha} \left(\frac{w}{1-\alpha}\right)^{1-\alpha}$
- Set prices subject to quadratic adjustment costs:

$$\Theta\left(\frac{\dot{p}}{p}\right) = \frac{\theta}{2} \left(\frac{\dot{p}}{p}\right)^2 Y$$



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Exact NK Phillips curve:

$$\left(r^{a}-\frac{\dot{Y}}{Y}
ight)\pi=rac{arepsilon}{ heta}\left(m-ar{m}
ight)+\dot{\pi},\quadar{m}=rac{arepsilon-1}{arepsilon}$$



#### Intermediate good firm pricing problem

$$\max_{\{p_t\}_{t\geq 0}} \int_0^\infty e^{-r^a t} \left\{ \Pi_t(p_t) - \Theta_t\left(\frac{\dot{p}_t}{p_t}\right) \right\} dt \quad \text{s.t.}$$

$$\Pi(p) = \left(\frac{p}{P} - m\right) \left(\frac{p}{P}\right)^{-\varepsilon} Y$$
$$m = \frac{1}{Z} \left(\frac{r}{\alpha}\right)^{\alpha} \left(\frac{w}{1-\alpha}\right)^{1-\alpha}$$
$$\Theta(\pi) = \frac{\theta}{2} \pi^2 Y$$

Back to firms



• Illiquid assets = part capital, part equity

a = k + qs

- k: capital, pays return  $r \delta$
- s: shares, price q, pay dividends  $\omega \Pi = \omega (1 m) Y$



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• Remaining  $(1 - \omega)\Pi$ ? Scaled lump-sum transfer to hh's:

$$\Gamma = (1 - \omega) \frac{z}{\bar{z}} \Pi$$



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CHICAGC

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• Set  $\omega = \alpha \Rightarrow$  neutralize asset redistribution from markups

total illiquid flow = 
$$rK + \omega \Pi = \alpha mY + \omega (1 - m)Y = \alpha Y$$

total liquid flow 
$$= wL + (1 - \omega)\Pi = (1 - \alpha)Y$$

# Monetary authority and government

• Taylor rule

$$i = \overline{r}^b + \phi \pi + \epsilon, \quad \phi > 1$$

with  $r^b := i - \pi$  (Fisher equation),  $\epsilon =$  innovation ("MIT shock")

• Progressive tax on labor income:

$$\tilde{T}(wz\ell+\Gamma) = -T + \tau(wz\ell+\Gamma)$$

• Government budget constraint (in steady state)

$$G-r^bB^g=\int \tilde{T}d\mu$$

• Transition? Ricardian equivalence fails ⇒ this matters!



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# Monetary Policy in Benchmark NK Models

Goal:

• Introduce decomposition of C response to r change

Setup:

- Prices and wages perfectly rigid = 1, GDP=labor = $Y_t$
- Households: CRRA( $\gamma$ ), income  $Y_t$ , interest rate  $r_t$

 $\Rightarrow C_t(\{r_s, Y_s\}_{s\geq 0})$ 

• Monetary policy: sets time path  $\{r_t\}_{t\geq 0}$ , special case

$$r_t = \rho + e^{-\eta t} (r_0 - \rho), \quad \eta > 0$$
 (\*)

- Equilibrium:  $C_t(\{r_s, Y_s\}_{s \ge 0}) = Y_t$
- Overall effect of monetary policy

$$-\frac{d\log C_0}{dr_0} = \frac{1}{\gamma\eta}$$



# Monetary Policy in RANK

• Decompose C response by totally differentiating  $C_0(\{r_t, Y_t\}_{t \ge 0})$ 

$$dC_0 = \underbrace{\int_0^\infty \frac{\partial C_0}{\partial r_t} dr_t dt}_{\text{direct response to } r} + \underbrace{\int_0^\infty \frac{\partial C_0}{\partial Y_t} dY_t dt}_{\text{indirect effects due to } Y}.$$

• In special case (\*)

$$-\frac{d \log C_0}{dr_0} = \frac{1}{\gamma \eta} \left[ \underbrace{\frac{\eta}{\rho + \eta}}_{\text{direct response to } r} + \underbrace{\frac{\rho}{\rho + \eta}}_{\text{indirect effects due to } Y} \right].$$

- Reasonable parameterizations  $\Rightarrow$  very small indirect effects, e.g.
  - $\rho = 0.5\%$  quarterly
  - $\eta = 0.5$ , i.e. quarterly autocorr  $e^{-\eta} = 0.61$

$$\Rightarrow \quad rac{\eta}{
ho+\eta}=99\%, \qquad rac{
ho}{
ho+\eta}=1\%$$



#### What if some households are hand-to-mouth?

- "Spender-saver" or Two-Agent New Keynesian (TANK) model
- Fraction  $\wedge$  are HtM "spenders":  $C_t^{sp} = Y_t$
- Decomposition in special case (\*)



•  $\Rightarrow$  indirect effects  $\approx \Lambda = 20-30\%$ 



## What if there are assets in positive supply?

- Govt issues debt B to households sector
- Fall in  $r_t$  implies a fall in interest payments of  $(r_t \rho) B$
- Fraction  $\lambda^{T}$  of income gains transferred to spenders
- Initial consumption restponse in special case (\*)

$$-\frac{d\log C_0}{dr_0} = \frac{1}{\gamma\eta} + \underbrace{\frac{\lambda^T}{1-\lambda \bar{Y}}}_{\text{fiscal redistribution channel}}$$

• Interaction between non-Ricardian households and debt in positive net supply matters for overall effect of monetary policy



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#### Solution Method (from Achdou-Han-Lasry-Lions-Moll)

- Solving het. agent model = solving PDEs
  - 1. Hamilton-Jacobi-Bellman equation for individual choices
  - 2. Kolmogorov Forward equation for evolution of distribution
- Many well-developed methods for analyzing and solving these
  - simple but powerful: finite difference method
  - COdeS: http://www.princeton.edu/~moll/HACTproject.htm
- Apparatus is very general: applies to any heterogeneous agent model with continuum of atomistic agents
  - 1. heterogeneous households (Aiyagari, Bewley, Huggett,...)
  - 2. heterogeneous producers (Hopenhayn,...)
- can be extended to handle aggregate shocks (Krusell-Smith,...) CHICAGO

#### Computational Advantages relative to Discrete Time

- 1. Borrowing constraints only show up in boundary conditions
  - FOCs always hold with "="
- 2. "Tomorrow is today"
  - FOCs are "static", compute by hand:  $c^{-\gamma} = V_b(a, b, \gamma)$
- 3. Sparsity
  - solving Bellman, distribution = inverting matrix
  - but matrices very sparse ("tridiagonal")
  - reason: continuous time  $\Rightarrow$  one step left or one step right
- 4. Two birds with one stone
  - tight link between solving (HJB) and (KF) for distribution
  - matrix in discrete (KF) is transpose of matrix in discrete (HJB)
- reason: diff. operator in (KF) is adjoint of operator in (HJB) CHICAGÔ

# HA Models with Aggregate Shocks: A Matlab Toolbox

- Achdou et al & HANK: HA models with idiosyncratic shocks only
- Aggregate shocks  $\Rightarrow$  computational challenge much larger
- Companion project: efficient, easy-to-use computational method
  - see "When Inequality Matters for Macro and Macro Matters for Inequality" (with Ahn, Kaplan, Winberry and Wolf)
  - open source Matlab toolbox online now see my website and https://github.com/gregkaplan/phact
  - extension of linearization (Campbell 1998, Reiter 2009)
  - different slopes at each point in state space



# Outline

#### 1. Model

2. Parameterization

#### 3. Results

#### 4. Additional Material

Literature Detailed Model Description Simple Model Solution Method

#### Balance Sheet Details

Earnings Dynamics Parameter Table Empirical Evidence



# Fifty shades of K

	Liquid	Illiquid	Total
Non-productive	Household deposits net of revolving debt Corp & Govt bonds $B^h = 0.26$		0.26
Productive		Indirectly held equity Directly held equity Noncorp bus equity Net housing Net durables	2.92 K
Total	$-B^{g} = 0.26$	A = 2.92	3.18

- Quantities are multiples of annual GDP
- Sources: Flow of Funds and SCF 2004
- Working paper: part of housing, durables = unproductive illiquid assets

back


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## Continuous time earnings dynamics

- Literature provides little guidance on statistical models of high frequency earnings dynamics
- Key challenge: inferring within-year dynamics from annual data
- Higher order moments of annual changes are informative
- Target key moments of one 1-year and 5-year labor earnings growth from SSA data
- Model generates a thick right tail for earnings levels



## Leptokurtic earnings changes



One-year change

Five-year change



## Two-component jump-drift process

• Flow earnings (y = wzI) modeled as sum of two components:

 $\log y_t = y_{1t} + y_{2t}$ 

- Each component is a jump-drift with:
  - mean-reverting drift:  $-\beta y_{it} dt$
  - jumps with arrival rate:  $\lambda_i$ , drawn from  $\mathcal{N}(0, \sigma_i)$
- Estimate using SMM aggregated to annual frequency
- Choose six parameters to match eight moments:



## Model distribution of earnings changes

Moment	Data	Model	Moment	Data	Model
Variance: annual log earns	0.70	0.70	Frac 1yr change < 10%	0.54	0.56
Variance: 1yr change	0.23	0.23	Frac 1yr change < 20%	0.71	0.67
Variance: 5yr change	0.46	0.46	Frac 1yr change < 50%	0.86	0.85
Kurtosis: 1yr change	17.8	16.5			
Kurtosis: 5yr change	11.6	12.1			

Transitory component:  $\hat{\lambda}_1 = 0.08$ ,  $\hat{\beta}_1 = 0.76$ ,  $\hat{\sigma}_1 = 1.74$ Persistent component:  $\hat{\lambda}_2 = 0.007$ ,  $\hat{\beta}_2 = 0.009$ ,  $\hat{\sigma}_2 = 1.53$ 





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Description		Value	Target / Source		
Prefere	nces				
λ	Death rate	1/180	Av. lifespan 45 years		
$\gamma$	Risk aversion	1			
$\varphi$	Frisch elasticity (GHH)	1			
$\psi$	Disutility of labor		Av. hours worked equal to 1/3		
ρ	Discount rate (pa)	5.1%	Internally calibrated		
Production					
ε	Demand elasticity	10	Profit share 10 %		
α	Capital share	0.33			
δ	Depreciation rate (p.a.)	7%			
θ	Price adjustment cost	100	Slope of Phillips curve, $\varepsilon/\theta = 0.1$		
Govern	ment				
au	Proportional labor tax	0.30			
Т	Lump sum transfer (rel GDP)	\$6,900	6% of GDP		
$\overline{g}$	Govt debt to annual GDP	0.233	government budget constraint		
Monetary Policy					
$\phi$	Taylor rule coefficient	1.25			
rb	Steady state real liquid return (pa)	2%			
Illiquid Assets					
r <sup>a</sup>	Illiquid asset return (pa)	5.7%	Equilibrium outcome		
Borrowing					
r <sup>borr</sup>	Borrowing rate (pa)	8.0%	Internally calibrated		
b	Borrowing limit	\$16,500	$\approx 1 \times$ quarterly labor inc		
Adjustment Cost Function					
$\chi_0$	Linear term	0.04383	Internally calibrated		
$\chi_1$	Coef on convex term	0.95617	Internally calibrated		
$\chi_2$	Power on convex term	1.40176	Internally calibrated		



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## **Evidence on MPCs from Norwegian lotteries**

Figure 4: Heterogeneous consumption responses. Quartiles of liquid and net illiquid assets



Source: Fagereng, Holm and Natvik (2016)

