## Measuring the Financial Soundness of U.S. Firms, 1926–2012\*

Andrew G. Atkeson,<sup>†</sup>Andrea L. Eisfeldt,<sup>‡</sup>and Pierre-Olivier Weill<sup>§</sup>

April 12, 2014

#### Abstract

We measure the distribution of firms' financial soundness over most of the last century for a broad cross section of firms. We highlight three main findings for this key aggregate state variable. First, the three worst recessions between 1926 and 2012 coincided with sharp deteriorations in the financial soundness of all firms, but other recessions did not. Second, fluctuations in total asset volatility, rather than fluctuations in leverage, appear to drive most of the variation in the distribution of firms' financial soundness. Finally, the distribution of financial soundness for large financial firms 1962-2007 largely resembles that for large nonfinancial firms.

<sup>\*</sup>Robert Kurtzman, David Zeke and Leo Li provided expert research assistance. We'd like to thank Tyler Muir and seminar participants at UCLA Anderson, the Federal Reserve Bank of Minneapolis, the Society for Economic Dynamics, Science Po Paris, UCL, Princeton, the Wharton liquidity conference, Duke Fuqua, the BU Boston Fed Macro Finance Conference, Berkeley Haas, UCSB, Claremont McKenna, Carnegie Mellon, Chicago Booth, Columbia GSB, MIT Sloan, the NBER Finance and Macroeconomics meeting, the Banque de France-Deutsche Bundesbank Conference on Macroeconomics and Finance Conference, the Real-Financial Linkages Workshop at the Bank of Canada, and the Finance and the Welfare of Nations conference at the Federal Reserve Bank of San Francisco for fruitful discussion and comments. We benefitted from the support of the National Science Foundation, grant SES-1260953. All errors are ours.

<sup>&</sup>lt;sup>†</sup>Department of Economics, University of California Los Angeles, NBER, and Federal Reserve Bank of Minneapolis. e-mail: andy@atkeson.net

<sup>&</sup>lt;sup>‡</sup>Finance Area, Anderson School of Management, University of California, Los Angeles, e-mail: andrea.eisfeldt@anderson.ucla.edu

<sup>&</sup>lt;sup>§</sup>Department of Economics, University of California Los Angeles, e-mail: poweill@econ.ucla.edu

## 1 Introduction

A large literature in macroeconomics argues that financial frictions impair the decisions of financially unsound firms and play a key role in amplifying and propagating business cycle shocks. Papers in this literature include Bernanke and Gertler (1989), Carlstrom and Fuerst (1997), Kiyotaki and Moore (1997), Bernanke, Gertler, and Gilchrist (1999), Cooley and Quadrini (2001), Cooley, Marimon, and Quadrini (2004), Jermann and Quadrini (2012), Covas and Den Haan (2011), and Kahn and Thomas (Forthcoming) and many others.<sup>1</sup> One key feature of models in this literature is that the distribution of financial soundness across firms in the economy at any point in time is an aggregate state variable that has important consequences for the response of the macroeconomy to a variety of aggregate shocks. In these models, heterogeneous firms choose output, employment, and investment, and, due to distorted incentives or expected bankruptcy costs, financial frictions adversely affect the decisions of financially unsound firms. As a result, negative macroeconomic shocks are greatly amplified and propagated when they simultaneously deteriorate the distribution of financial soundness across firms.

Motivated by the literature cited above, in this paper, we propose a contribution to the measurement of this key aggregate state variable, the *aggregate distribution of firms' financial soundness*. We start by developing and empirically validating a procedure for measuring the financial soundness of each publicly traded firm in the U.S. economy that we call *Distance to Insolvency*, or *DI*. This measure is theoretically grounded in a simple structural model of firms' based on the work of Leland (1994). In this model, DI measures a firm's leverage adjusted for the volatility of its underlying assets. Put differently, for each firm in the economy, DI is a measure of the adequacy of that firm's equity cushion relative to its business risk. We show theoretically that one can approximate a firm's DI using data on the inverse of the volatility of individual firms' equity returns and we show empirically that the signal of a firms' financial soundness derived from the volatility of its equity returns is highly correlated with alternative signals of firms' financial soundness studied in the literature including those derived from credit ratings, bond spreads, spreads on credit default swap rates, and bond default rates for those firms and time periods for which these alternative signals are available.

We then use data on equity volatility to approximate DI on a firm-by-firm basis monthly for all publicly traded firms in the CRSP daily database, and, in this way, we create a monthly time series for the cross-section distribution of DI across all publicly traded firms in the U.S. economy over the 87 years from 1926-2012. This exercise allows us to make two contributions to measurement. First, we are able to construct a theoreti-

 $<sup>^1</sup>$ Ben Bernanke delivered a speech summarizing this literature in 2007 available at http://www.federalreserve.gov/newsevents/speech/bernanke20070615a.htm

cally grounded measure of the financial soundness of a broader cross section of firms over a longer historical time period than has been done previously in the literature with alternative market signals of firms' financial soundness. In particular, we are able to directly compare the evolution of the distribution of financial soundness across firms during the Great Depression with that during the postwar period including the most recent financial crisis. Second, we can use our structural model to present a novel decomposition of the proximate drivers of movements in this cross section distribution of firms' financial soundness into movements due to changes in firms' leverage and to changes in two components of firms' business risk: a component of risk that is common to all firms and a component of risk that is idiosyncratic to each firm.

We emphasize three main empirical findings regarding this evolution of the crosssection distribution of firms' financial soundness.

Our first main finding is that over the 1926-2012 time period, there are a number of episodes in which the entire distribution of measured DI across publicly traded firms in the United States deteriorated sharply. We term these episodes insolvency crises. In particular, we define insolvency crises as months in which the median measured DI in that month's cross section of measured DI across firms drops to a level normally associated with extreme financial distress, and the 95th percentile of measured DI drops to a level normally associated with junk credit ratings or worse. We find that the largest recessions in our sample, namely 1932–1933, 1937, and 2008, are closely associated with insolvency crises. However, we do not find significant insolvency crises in other recessions outside of these three. This includes even the deep recessions of the late 1970s and early 1980s. These findings are not sensitive to the cutoffs used to define insolvency crises — the insolvency crises of 1932–33, 1937, and 2008 are quite distinctive events in the data. These findings are consistent with the hypothesis that a sharp deterioration in the financial soundness of most, if not all firms played a major role in three of the largest recessions in U.S. history. At the same time, these findings cast doubt on the importance of changes in the distribution of financial soundness for a broad cross section of firms for U.S. postwar recessions outside of the most recent one.<sup>2</sup>

To obtain our second main empirical finding we decompose the proximate drivers of changes in the distribution of measured DI across firms into movements due to changes in firms' leverage and changes to two components of firms' business risk: a component of risk that is common to all firms and a component of risk that is idiosyncratic to each firm. A significant literature points to the buildup of leverage across firms as a key precursor to the start of a financial crisis (see, for example, Kindleberger and Aliber, 2005, and Reinhart

 $<sup>^{2}</sup>$ See Giesecke, Longstaff, Schaefer, and Strebulaev (2011) for a related quantitative finding based on bond default rates.

and Rogoff, 2009). Typically, in the literature cited in our first paragraph, the proximate cause of the deterioration of firms' financial soundness is a further increase in firms' leverage precipitated by a drop in the value of firms' assets or collateral. The impact of changes in firms' business risk or asset volatility on firms' financial soundness, on the other hand, has been examined more closely only recently, for example, by Christiano, Motto, and Rostagno (2010), Gilchrist, Sim, and Zakrajsek (2010), Rampini and Viswanathan (2010), Arellano, Bai, and Kehoe (2011), and others.<sup>3</sup> For the time period 1972–2012, we can use accounting data from COMPUSTAT in order to measure separately the leverage and asset volatility components of DI. This allows us to examine the role of changes in firms' leverage versus changes in firms' asset volatilities in accounting for the changes in the distribution of firms' measured DI over this time period, in particular during the insolvency crisis of 2008.

Contrary to many theories of financial crises cited above, we find that the deterioration of firms' measured DI during the insolvency crisis of 2008 was mainly due to an increase in asset volatility for all firms. The contribution of the increase in leverage, induced either by "excessive borrowing" in advance of the crisis or a fall in asset values during this insolvency crisis, was relatively small. In fact, over the entire period for which we have the COMPUSTAT accounting data needed to compute firms' leverage, we find that changes over time in the distribution of measured DI across firms are mainly a result of changes in the volatility of firms' underlying assets rather than of changes in firms' leverage.<sup>4</sup> Moreover, one of the striking features of the insolvency crises that we observe in the data is that all firms appear to be impacted, including firms that have little or no financial leverage.<sup>5</sup> In the most recent financial crisis in particular, we find that the deterioration in DI that occurred for firms with no long term financial debt is very similar to that which occurred for firms with long-term financial debt. Our second finding complements recent work by Bloom (2009), Bloom, Floetotto, Jaimovich, Saporta, and Terry (2013), and others, which demonstrates large contractions in aggregate activity from changes in asset volatility directly.<sup>6</sup>

 $<sup>^{3}</sup>$ A notable earlier exception is Williamson (1987) who introduces business cycle variation in project risk into the costly state verification framework of Townsend (1979).

<sup>&</sup>lt;sup>4</sup>Related findings appear in the contemporaneous work by Choi and Richardson (2013) on the decomposition of levered equity returns with stochastic volatility. They study the movement of equity volatility on a firm-by-firm basis rather than the movement of the overall distribution of equity volatility across firms. Their findings corroborate the greater relative contribution to changes in equity volatility of changes in asset volatility relative to changes in leverage, except, in their firm level data, for the most levered firms.

<sup>&</sup>lt;sup>5</sup>In our structural model of firms' distance to insolvency, fixed operating costs, i.e. operating leverage, are mathematically equivalent in the theory to financial leverage.

 $<sup>^{6}</sup>$ Recent related empirical work by Jurado, Ludvigson, and Ng (2013) provides a measure of uncertainty by measuring the volatility of the unforecastable component of macroeconomic time series.

The rapidly growing literature in macroeconomics that examines the role of changes in business risk as measured by changes in asset volatility in driving macroeconomic fluctuations can be divided into two parts. One part of this literature emphasizes factors such as time variation in the market price of risk<sup>7</sup> or in aggregate disaster risk<sup>8</sup> that impact the volatility of a common component of the innovations to asset values for all firms. A second and more recent part of this literature cited above emphasizes variation in the distribution of financial soundness across firms due to time variation in the variance of the idiosyncratic or firm-specific component of innovations to asset valuations for all firms. Following Campbell et al. (2001), Gilchrist, Sim, and Zakrajsek (2010), and Kelly, Lustig, and Van Nieuwerburgh (2012), we decompose the volatility of innovations to firms' asset values into a portion of that volatility due to a common component of these innovations and a portion of the volatility due to an idiosyncratic component of these innovations. Consistent with the results in Kelly et al. (2012), we find that fluctuations in the volatility of the idiosyncratic component of innovations to firms' asset values for all firms account for most of the movement in the cross section distribution of financial soundness across firms, particularly in the most recent financial crisis. Movements in the common component of innovations to the value of firms' assets are less important as a driver of movements in the cross section distribution of firms' financial soundness over time.

On the basis of these findings, we argue that in order to understand insolvency crises, one must account for changes in the volatility of the idiosyncratic component of firms' asset volatility that simultaneously impact all firms in the economy, whether they have financial leverage or not.

For our third main empirical finding, we examine the differences in the movements of the distribution of financial soundness for large financial firms versus large non-financial firms. The macroeconomic literature cited above highlights the role of financial frictions facing *all firms* in shaping business cycles. Another large literature in macroeconomics makes the case that frictions facing *financial intermediaries* play perhaps an even larger role in shaping the evolution of the macroeconomy. According to this literature, recessions can be caused by a deterioration in the financial soundness of financial intermediaries alone, due to their central role in reallocating resources in the economy.<sup>9</sup> One of the

<sup>&</sup>lt;sup>7</sup>See, for example, the models of intermediary asset pricing in Brunnermeier and Sannikov (2012), He and Krishnamurthy (2013), and Muir (2013), or the model of equilibrium credit spreads and consumption volatility in Gomes and Schmid (2010).

<sup>&</sup>lt;sup>8</sup>See, for example, Rietz (1988), Barro (2006), Gabaix (2012), and Gourio (Forthcoming).

<sup>&</sup>lt;sup>9</sup>An important early paper is Bernanke (1983). Gertler and Kiyotaki (2010) surveys recent theoretical contributions, and the empirical experience with financial crises is described in Reinhart and Rogoff (2009). Additional recent work focusing on the distinct role of the intermediary sector in business cycle contractions in real activity includes Cúrdia and Woodford (2009), Brunnermeier and Sannikov (2012), Gilchrist and Zakrajšek (2012), Gertler and Karadi (2011), and Rampini and Viswanathan (2012).

main virtues of our proposed method for measuring the financial soundness of firms is that it can easily be applied to financial as well as nonfinancial firms even though the type and reporting of leverage in financial statements vary considerably across the two types of firms. We find that the financial soundness of large publicly traded financial firms closely resembles that of large nonfinancial firms for the entire period of 1962 to July 2007.<sup>10</sup> In particular, in advance of the most recent financial crisis, we find that the market perceived both large financial and non-financial firms to be at a historically high level of financial soundness. Empirically, then, we see little or no evidence that the many changes in financial regulation that occurred over this time period played a significant role in leading large financial institutions to take on significantly more leverage than their non-financial peers in the run-up to the most recent crisis once leverage is adjusted by the market's perceptions of each type of firms' business risk.

The remainder of this paper is organized as follows. In section 2, we describe the theory underlying our measurement procedure. In section 3 we compare the empirical performance of our measure of firms' distance to insolvency to alternative measures of firms' financial soundness. We then turn to an analysis of the characteristics of the distribution of distance to insolvency across firms as our aggregate state variable of interest. In section 4 we present our empirical results regarding our three questions on the relationship between insolvency crises and business cycles. We conclude in section 5 with a discussion of the implications of these findings for business cycle research. A supplementary appendix provides additional theoretical and empirical results.

## 2 The Theory Underlying Our Measurement

Our empirical work has its theoretical foundations in the structural models of firms' credit risk pioneered by Merton (1974) and Leland (1994). In those models, a key state variable summarizing a firm's financial soundness is Distance to Insolvency, or DI: a measure of the firm's leverage adjusted by the volatility of innovations to the market valuation of its underlying assets. DI is a key state variable both in a statistical sense — it summarizes the probability that the firm will become insolvent in the future<sup>11</sup> — and in an economic sense because it summarizes the distortions to equity holders' incentives that potentially

 $<sup>^{10}</sup>$ The number of publicly traded financial firms is very small before 1962 and thus we are not able to present meaningful results for the 1926-1961 time period.

<sup>&</sup>lt;sup>11</sup>A large literature uses a related measure of firms' leverage adjusted for asset volatility computed from the Merton model to forecast firms' bond default and bankruptcy rates in a reduced-form manner. Duffie (2011) clearly describes one way in which this procedure can be implemented. Moody's Analytics (a subsidiary of the credit rating agency) has sold the results from a related model under the brand name *Expected Default Frequency*, or EDF, for over a decade. The specification of their model and its empirical implementation are described in Sun, Munves, and Hamilton (2012).

arise when the firm becomes financially distressed.<sup>12</sup>

In this section we use a straightforward extension of Leland's (1994) structural model of credit risk in order to derive two approximation results that dramatically simplify measurement relative to what has been done in the academic literature and in commercial applications. We show that one can approximate a firm's DI simply with the inverse of its instantaneous equity volatility. Specifically, we show that in the Leland's model of credit risk, at any point in time, inverse equity volatility *is an upper bound on the firm's DI*. Second, we show that if the firm's creditors are aggressive in forcing the equity holders to file for bankruptcy as soon as the firm is insolvent, then *this upper bound is tight.*<sup>13</sup> We argue that because these findings rely on just a few elementary properties of the value of equity, they are likely to hold in a broad class of models.

#### 2.1 Distance to Insolvency: Definition

To define terms, we make use of the following notation. On the left-hand side of the firm's balance sheet are assets that yield at time  $t \ge 0$  a stochastic cash flow denoted by  $y_t$ . Let  $V_{At}$  be the market value of the assets' future cash flows, measured using state-contingent prices. On the right-hand side of the firm's balance sheet are liabilities, that we model as a deterministic sequence of cash flows  $\{c_t, t \ge 0\}$  that the equity holders of the firm are contractually obligated to pay if they should wish to continue as owners of the firm. Let  $V_{Bt}$  be the market value of the liabilities' future cash flows, valued as if they were default free. Of course, since the firm may default on its liabilities,  $V_{Bt}$  is larger than the market value of the firm's debt. We say that a firm is *solvent* if its underlying assets are worth more than the promised value of its liabilities,  $V_{At} \ge V_{Bt}$ , and *insolvent* otherwise. Let the *asset volatility*,  $\sigma_{At}$ , be the (instantaneous) annualized percentage standard deviation of innovations to  $V_{At}$ , representing the business risk that the firm faces. Let the firm's underlying assets and the

<sup>&</sup>lt;sup>12</sup>To generate real costs of financial distress, these models rely on some violation of the Modigliani and Miller theorem (Modigliani and Miller, 1958). Myers (1977) is an early contribution characterizing the cost of debt financing arising from suboptimal investment. Townsend (1979) studies optimal financing under asymmetric information and shows that debt financing minimizes monitoring costs. Diamond and He (forthcoming) shows that investment distortions due to debt overhang vary with debt maturity, and they derive the optimal debt maturity structure. Villamil (2008) presents a survey of some of the important theoretical work that derives violations of Modigliani and Miller from the underlying constraints on contracting and information. Recent work by Hackbarth et al. (2006), Almeida and Philippon (2007), Chen et al. (2009), Chen (2010), Bhamra, Kuehn, and Strebulaev (2010), and Gomes and Schmid (2010) emphasizes the time-varying nature of the costs of financial distress.

 $<sup>^{13}</sup>$ Black and Cox (1976) pioneered the study of structural models of credit risk in which creditors add bond provisions to force equity to exercise their right to limited liability when the firm becomes insolvent. Longstaff and Schwartz (1995) build on the Black and Cox model to incorporate both default and interest rate risk.

firm's liabilities,  $\frac{V_{At}-V_{Bt}}{V_{At}}$ . A firm's *Distance to Insolvency*, or DI, is defined as the ratio of our measure of leverage to our measure of asset volatility, both dated at a point in time t:

$$DI_t \equiv \left(\frac{V_{At} - V_{Bt}}{V_{At}}\right) \frac{1}{\sigma_{At}}.$$
(1)

This ratio corresponds to the drop in asset value that would render the firm insolvent, measured in units of the firm's asset standard deviation.

We illustrate these concepts graphically in Figure 1. The solid blue line in the figure denotes the evolution of the value of the firm's assets,  $V_{At}$ , over time. The solid blue line ends at the current time t. The solid red line denotes the value of the firm's promised liabilities  $V_{Bt}$ . The black arrow denotes the distance between  $V_{At}$  and  $V_{Bt}$  at time t. The dashed blue lines denote standard error bands around the evolution of  $V_{At+s}$  going forward at different time horizons s > 0. The likelihood that the firm becomes insolvent in the near term depends on both the distance between  $V_{At}$  and  $V_{Bt}$ , measured here in percentage terms by the firm's leverage, and the volatility in percentage terms of innovations to the value of the firm's assets. We combine these two factors into DI, which serves as simple one-dimensional index of the firm's financial soundness.

#### 2.2 Distance to Insolvency: Measurement

Calculating a firm's DI is challenging in practice because it requires one to measure separately the market value and volatility of a firm's underlying assets,  $V_{At}$  and  $\sigma_{At}$ , and the value of its liabilities,  $V_{Bt}$ . The former are not directly observable, and the latter is subject to deficiencies and inconsistencies in accounting measures of firms' liabilities across countries, time, and industries.

One approach to this measurement problem, pioneered by Merton (1974) and Leland (1994), is to use a specific structural model of the cash flows from the firm's assets and accounting data on the firm's liabilities, together with assumptions about the interest rates and risk prices used to discount those cash flows. Equipped with such a model, one can derive formulas for the value of the firm's equity at t, denoted by  $V_{Et}$ , and the standard deviation of the innovations to the logarithm of  $V_{Et}$ , denoted by  $\sigma_{Et}$ , as functions of the asset value and volatility and the firm's liabilities,  $V_{At}$ ,  $\sigma_{At}$ , and  $V_{Bt}$ . Given market data on the firm's equity value and equity volatility, and accounting data on the firm's liabilities, one can then invert these formulas to uncover the unobserved asset value  $V_{At}$  and asset volatility  $\sigma_{At}$ . Duffie (2011) clearly describes one way in which this procedure can be implemented using the Merton model.

Our theoretical results below show that one can approximate DI in a simple way using

only equity volatility data.

The benchmark Leland Model. In the benchmark Leland (1994) model, we make the following assumptions. Let interest rates and the market price of risk be constant. The cash flows derived from the firm's underlying assets (lines of business) follow a geometric Brownian motion with constant volatility. In this case, the market value of the firm's asset,  $V_{At}$ , also follows a geometric Brownian motion with constant volatility. In this case, the market volatility  $\sigma_A$ . In particular, fluctuations in  $V_{At}$  are driven entirely by fluctuations in the firm's projected cash flows. On the right of its balance sheet, the firm has liabilities given by a perpetual constant flow of payments c > 0. Hence, the present value of these payments is constant and equal to  $V_B = c/r$ , where r > 0 denotes the interest rate.

Equity holders have limited liability, in that they can choose to stop making the contractual liability payments, in which case they default and assets are transferred to creditors. Creditors may be protected by covenants, allowing them to force equity holders into default if the value  $V_{At}$  of the assets falls below some exogenously given threshold, which we assume is lower than  $V_B$ . Using standard arguments, one can show that, when the value of assets falls below some threshold  $V_A^* \leq V_B$ , either equity holders exercise their right to default or creditors exercise their protective covenants.

The value of equity can be written as  $V_{Et} = w(V_{At})$ , for some continuous function  $w(V_A)$  with three key properties presented in the next lemma and illustrated in Figure 2.

**Lemma 1.** In the Leland (1994) structural model, the value of equity,  $w(V_A)$ , is greater than  $\max\{0, V_A - V_B\}$ , nondecreasing, convex, and satisfies  $w'(V_A) \leq 1$  as well as  $w(V_A^*) = 0$ .

The lower bound on equity's value,  $\max\{0, V_A - V_B\}$ , follows from the limited liability assumption: the value of equity has to be greater than zero, and it also has to be greater than  $V_A - V_B$ , its value under unlimited liability. Moreover, in line with the original insights from Merton (1974), the value of equity inherits the standard convexity properties of call options.<sup>14</sup> Note in particular that  $w'(V_A) \leq 1$ , which follows from the fact that the option value of limited liability falls as the value of the firm's assets rises. Finally, the value of equity must be zero at the default point,  $V_A^*$ .

Armed with these basic properties for the value of equity, we develop our two approximation results that relate distance to insolvency and leverage adjusted for asset volatility. We show each result in turn.

<sup>&</sup>lt;sup>14</sup>The Merton model differs from the Leland model only in the assumption that the cash flows on liabilities are simply a single cash flow required at a specific date T in the future. This lemma also applies to the value of equity in the Merton model at dates t < T with the change that the default threshold is time-varying with  $V_{At}^{\star} = 0$  for t < T and  $V_{AT}^{\star} = V_{BT}$ .

**Proposition 1.** In a Leland (1994) structural model, Distance to Insolvency bounded above by the inverse of equity volatility:

$$DI_t = \left(\frac{V_{At} - V_B}{V_{At}}\right) \frac{1}{\sigma_A} \le \frac{1}{\sigma_E}$$

*Proof.* To prove this result, note first that, by Ito's formula, the volatility of equity solves:

$$\sigma_{Et} = \frac{w'(V_{At})}{w(V_{At})} \sigma_A V_{At} \Longrightarrow \frac{1}{\sigma_{Et}} = \frac{w(V_{At})}{w'(V_{At})} \frac{1}{\sigma_A V_{At}}.$$

By Lemma 1 we have that  $w(V_{At}) \ge V_{At} - V_{Bt}$ , and  $w'(V_{At}) \le 1$ , and the results follow.  $\Box$ 

Next, consider the question of whether this upper bound on a firm's DI is tight. To do this, recall that  $V_A^*$  is the threshold asset value at which equity exercises its option to default: it gives up control of the firm's assets in exchange for abandoning the firm's liabilities. We use  $V_A^*$  to define the concept of *Distance to Default*, or DD, in our benchmark Leland model as

$$DD_t = \left(\frac{V_{At} - V_A^*}{V_{At}}\right) \frac{1}{\sigma_A}.$$
(2)

Note that default is distinct from insolvency in our theory and that quite generally a firm's DD exceeds its DI. This is because equity may not walk away immediately from an insolvent firm, but will not choose default if the firm is solvent. With this definition we have our second proposition.

**Proposition 2.** In a Leland (1994) structural model, the inverse of a firm's equity volatility lies between its Distance to Insolvency and its Distance to Default:

$$DI_t \le \frac{1}{\sigma_{Et}} \le DD_t.$$

*Proof.* This proposition follows from the convexity of the value of the firm's equity as a function of the value of the firm's assets at each time t and because  $w(V_A^*) = 0$ .

We illustrate the proof of these two propositions in Figure 2. At time t, the value of the firm's equity as a function of the value of its assets is a convex function with slope less than or equal to one that lies above the horizontal axis (exceeds zero) and the line  $V_{At} - V_B$  giving the value of the firm's equity under unlimited liability. The value of the firm's equity hits the horizontal axis at the default point  $V_A^*$ . Define  $X_t$  to be the point at which the tangent line to the value of equity  $V_{Et}$  at the current asset value  $V_{At}$  hits the x-axis. All these lines and points are drawn in this figure.

By the convexity of  $w(V_A)$ , we have  $V_A^* \leq X_t \leq V_B$ . Simple algebra then delivers that

$$\frac{1}{\sigma_{Et}} = \left(\frac{V_{At} - X_t}{V_{At}}\right) \frac{1}{\sigma_A},$$

which proves the result.

With these two results, we have that the inverse of a firm's equity volatility,  $1/\sigma_{Et}$ , is an accurate measure of Distance to Insolvency if the Distance to Insolvency and the Distance to Default are close to one another. That is, the bound is tight if creditors quickly force insolvent firms into default. Therefore, as an empirical matter, the economics of creditors' incentives to force a firm that is insolvent into bankruptcy as soon as possible to avoid further costs of financial distress suggests that firms with alert and aggressive creditors should satisfy this condition. Regardless of the tightness of the bound, our procedure for measuring DI should be conservative in identifying firms' financial distress because inverse equity volatility is an upper bound on DI.

Although we have established our approximations in the context of a simple model, our results rely on just a few elementary properties of the value of equity, which are likely to hold in a broad class of models used in applied work. First, the proof requires that the value of equity be a convex function of the value of assets with slope less than one, a property that is typical of structural credit risk models. Second, the proof requires that the value of equity is the only state variable following a diffusion. Thus, our results hold if there are other state variables, for the interest rate, market price of risk, or liability payments, as long as these are "slower moving" in the sense of being continuous-time Markov chains.<sup>15</sup>

Based on these theoretical results, in the empirical work that follows, we approximate a firm's DI by the inverse of its equity volatility,  $1/\sigma_{Et}$ . We term this approximation "measured DI". We estimate  $1/\sigma_{Et}$  monthly by the inverse of realized volatility, which we compute from the CRSP database on daily equity returns for each firm and each month from 1926 to 2012.<sup>16,17</sup> One may argue that, since the concept of financial soundness is

<sup>&</sup>lt;sup>15</sup>See for example Hackbarth, Miao, and Morellec (2006) and Chen (2010) for versions of Leland's model in which the firm's cash flow process follows, under the risk-neutral measure, a modulated geometric Brownian motion. See Chen et al. (2009) for a structural model with time-variation in the market price of risk and in the variance of the idiosyncratic component of business risk.

<sup>&</sup>lt;sup>16</sup>The CRSP daily data set on equity returns includes NYSE daily data beginning December 1925, Amex (formerly AMEX) daily data beginning July 1962, NASDAQ daily data beginning December 1972, and ARCA daily data beginning March 2006. We estimate  $\sigma_{Et}$  for a firm in a given month t by the square root of the average squared daily returns in the month. We annualize this standard deviation by multiplying by  $\sqrt{252}$  where 252 is the average number of trading days in a year.

<sup>&</sup>lt;sup>17</sup>One could also compute realized volatility using a range of alternative methods including a rolling window of returns, or the latent-variable approach of stochastic volatility models. We have chosen our measure primarily to ensure that it does not use overlapping daily data and for the convenience of correspondence with the monthly calendar.

fundamentally forward looking, DI should be measured using implied instead of realized volatility. An important drawback of using implied volatility, however, is that it is available only for selected stocks, and only for recent dates. Moreover, in Appendix D, we compare the distribution of realized versus implied volatilities, for the available data, and we show that the two track each other closely. We conclude that the benefits of using realized volatility largely outweigh the costs.

## 3 Distance to Insolvency and Alternative Measures of Financial Soundness

In this section we compare our measure of DI, based on equity volatility, to leading alternative measures of firms' financial soundness for those time periods in which we have data for these alternative measures.

First, we construct a mapping between the level of measured DI and Standard and Poor's credit ratings in the cross section. We use this mapping to interpret the level of measured DI in terms of these credit ratings.

We next validate our calibration of measured DI using credit ratings by comparing it to option adjusted bond spreads and credit default swap rates. In our structural model, all of these market signals are signals of firms' underlying DI and thus should be highly correlated. Specifically, we compare the median measured DI to the median optionadjusted bond spreads, and to the median credit default swap rate, every month within portfolios of firms sorted by credit ratings.<sup>18</sup>

We find that the logarithm of median measured DI for these portfolios has a strong linear relationship with both the logarithm of median option-adjusted bond spreads, and the logarithm of median credit default swap rates.<sup>19</sup> This relationship is roughly stable both in the cross section and in the time series even through the time period encompassing the most recent financial crisis. This approximate stability over time of the relationship between firms' measured DI and bond spreads and CDS spreads corroborates our argument that one can construct a measure of insolvency crises based on the unconditional

<sup>&</sup>lt;sup>18</sup>By organizing firms into these portfolios based on credit ratings, we are able to reduce the impact of sampling error in the estimation of firms' equity volatility on the empirical relationship between these alternative measures. We see this use of portfolios rather than individual firms as particularly important for our empirical purposes since we are interested in measuring the distribution of financial soundness across a broad cross section of firms rather than in measuring the financial soundness of any particular firm.

<sup>&</sup>lt;sup>19</sup>Our findings here that measured DI and credit spreads are closely associated corroborates finance industry pricing and hedging practices as summarized in the CreditGrades model described in Finkelstein et al. (2002), as well as the findings in Campbell and Taksler (2003), Schaefer and Strebulaev (2008), and Gilchrist, Sim, and Zakrajsek (2010).

level of an economy-wide measure of DI.

#### 3.1 Measured DI and Credit Ratings

To interpret the level of measured DI, we first study its cross-sectional relationship with credit ratings. Specifically, we compare the inverse of firms' equity volatility to their credit ratings as reported quarterly in COMPUSTAT. We pool all firm-month observations from 1985 to the present for which we simultaneously have a credit rating from COMPUSTAT and daily stock return data from CRSP. Each month, we place firms into credit ratings bins and then compute the median measured DI for all firm-month observations by ratings bin.

These data reveal a clear monotonic relationship between the two: highly rated firms have a higher median measured DI.<sup>20</sup> We emphasize four cutoffs for mapping measured DI into credit ratings. For highly rated firms (A and above), the median measured DI is 4. For firms at the margin between investment grade and speculative grade (BBB-vs. BB+), the median DI is 3. For firms that are vulnerable (in the B range), the median measured DI is 2, whereas for firms that have filed for bankruptcy and/or have defaulted (C or D), the median measured DI is 1.<sup>21</sup>

In further support of our calibration, we find that the frequency of firms having an investment grade rating increases sharply with measured DI for rated firms: it is less than 15% if measured DI is below 1, and more than 80% if measured DI is above 4.<sup>22</sup> For measured DI's between 1 and 2, this probability is 30%, for measured DI's between 2 and 3, it is just under 50% and finally for measured DI's between 3 and 4, it is 65%. Thus, a measured DI below 1 strongly indicates that a firm has a speculative grade rating, and a measured DI above 4 strongly indicates a firm has an investment grade rating.

Finally, we also consider the frequency in the pooled firm-month data of firms being what S&P calls "highly vulnerable" (a rating of CC and below), conditional on values of DI. For firms with measured DI less than 1, this frequency is about 10% and for firms with measured DI's between 1 and 2, it is about 1.4%. To interpret these conditional probabilities, note that the unconditional probability of a rating CC and below is very small, about 0.75%. Taking this into account, a firm with measured DI below 1 is thirteen

 $<sup>^{20}</sup>$ Figure S2, shown in the supplementary appendix, plots the median of the cross-sectional distribution of firms' measured DI conditional on Standard & Poors (S&P) credit rating.

<sup>&</sup>lt;sup>21</sup>In fact, our data indicates that monotonicity holds not only for the median, but for all percentiles. This means that, in the cross-section, a higher credit rating corresponds to a higher measured DI, in the sense of first-order stochastic dominance.

<sup>&</sup>lt;sup>22</sup>Figure S3, shown in the supplementary appendix, plots the frequency in the pooled firm-month data of firms having an investment grade rating (BBB- and above) conditional on values of measured DI. It is important to note that the unconditional distribution of firms' credit ratings is biased towards higher ratings since firms select into being rated.

times more likely to be highly vulnerable than a randomly chosen firm. A firm with a measured DI between 1 and 2 is twice more likely to be highly vulnerable.

Given these findings, we propose the following benchmark calibration to interpret the level of measured DI:

- measured DI above 4: good and safe.
- measured DI of 3: borderline between investment and speculative grade.
- measured DI of 2: vulnerable.
- measured DI below 1: highly vulnerable.

#### **3.2** Measured DI and Bond Credit Spreads

We now consider the relationship between measured DI and credit spreads in bond yield data. Bank of America-Merrill Lynch (BAML) calculates daily data on option-adjusted bond spreads<sup>23</sup> for a large universe of corporate bonds whose yields underlie BAML's corporate bond indices. BAML then groups firms into portfolios by rating class, for the seven ratings classes AAA to CCC and below and reports an index of the option-adjusted spread on bonds of firms in each portfolio. These daily data on option adjusted bond spreads by ratings class are available from 1997 to 2012.<sup>24</sup> We compute monthly averages of daily option-adjusted spreads on these indices and, in Figure 3, we plot the logarithm of these option adjusted bond spreads against the logarithm of median measured DI for firms in the same ratings class bin in the same month. We plot separately the pre–August 2007 data (with blue triangles) and post–August 2007 data (with red circles). Note two sources of variation are shown in this figure: variation in measured DI and bond spreads across credit ratings classes at a point in time and variation over time in measured DI and bond spreads by ratings class.

Clearly, credit spreads are decreasing in measured DI, and the relationship is linear in logs. This relationship is relatively tight: the  $R^2$ 's from a regression of log optionadjusted spread on log measured DI for data pre– and post–August 2007 are 0.74 and 0.79, respectively. For another way to see that measured DI is strongly indicative of credit spreads, consider that having a low measured DI and a low credit spread is very rare. In particular, no portfolio has a measured DI below 1 and an option-adjusted spread below 400bp. Likewise, it is very rare to have a high measured DI (above 4) and a high

<sup>&</sup>lt;sup>23</sup>The option adjustment here is intended to correct bond spreads for features of corporate bonds, such as callability, that do not correspond to default risk and yet might impact observed bond spreads.

<sup>&</sup>lt;sup>24</sup>These data are available in the data repository FRED at the Federal Reserve Bank of St. Louis.

credit spread (above 400bp). We conclude from the data on measured DI and optionadjusted spread, that measured DI captures a significant amount of the information in credit spreads, and this helps to validate DI as a measure of financial soundness.

Note as well that the linear relationship in logs between measured DI and bond spreads is relatively stable in the data pre–August 2007 and post–August 2007. We interpret this finding as indicating that during the financial crisis of 2008, both measured DI and bond spreads as indicators of financial soundness deteriorated over time in the same relative proportion as they do typically at a point in time across the spectrum of firms of different credit qualities.

#### 3.3 Measured DI and Credit Default Swap Rates

In the past decade, a broad market in credit default swaps has emerged. Credit default swaps have a payoff, contingent upon default, that is equal to the value of the defaulted bond relative to its face value. Thus, CDS rates offer a natural market-based measure of corporate default risk which we can compare to measured DI.

We use data from Markit on single-name five-year CDS rates from 2001 through 2011. We construct monthly averages of daily swap rates by firm. We then merge this CDS swap rate data with our monthly DI data from CRSP by CUSIP using Markit's Reference Entity Dataset, then hand and machine-check the results of our merge. Finally, we bin firms by ratings class into seven ratings classes from AAA to CCC and below to reduce noise, and we compute the median CDS rate and median measured DI monthly by rating class.

Figure 4 plots measured DI versus CDS rates by ratings class for 2001–2011. We use a log scale because the relationship between measured DI and CDS rates is, like the relationship between measured DI and option-adjusted bond spreads, close to log linear. The plot shows a clear negative relationship between CDS rates and measured DI. It also adds further credibility to our calibration, since relatively few observations with a measured DI less than 2, and very few observations with a measured DI less than 1, correspond to a CDS rate below 400bp. Conversely, very few observations have a measured DI greater than 4 and a CDS rate above 200bp. We separate the data pre– August 2007 and post–August 2007 to support the claim that our calibration in levels that are constant over time. The  $R^2$  from a regression of log CDS rate on log measured DI is 0.76 for the data pooled by credit rating pre–2007 and 0.67 post–2007.<sup>25</sup> Although the slope and intercept coefficients differ across these two samples, our calibration appears robust, since in both time periods a measured DI below 1 corresponds to a CDS rate of 400bp, and a DI above 4 corresponds to a CDS rate below 200bp.

 $<sup>^{25}</sup>$ The same regression using firm-level data for the whole sample yields similar coefficients and an  $R^2$  of over 30%.

#### **3.4** Measured DI and Bankruptcy

To confirm that measured DI has implications for real outcomes, we also briefly document the relationship between measured DI and bankruptcy.<sup>26</sup> For our purposes, we establish two facts. First, in the cross section, we show that DI decreases monotonically as firms become closer and closer to bankruptcy. This corroborates our calibration. Then, in the time series, we show that the fraction of firms with low measured DI is strongly correlated with the aggregate default rate. Thus, even though measured DI is based on market prices, and is thus driven by both fundamental risk and potentially time-varying risk premia, measured DI and actual default events are related both in the cross section and in the time series. In the supplementary appendix we show a strong monotonic relationship between DI and *Black and Scholes' Distance to Default* (DD), which is commonly used in forecasting individual firms' bond default and bankruptcy rates (see, for example, Duffie, 2011; Sun, Munves, and Hamilton, 2012). We interpret this finding as indicating that measured DI should also be a strong indicator of firms' bond default and bankruptcy risk.

We first examine the evolution of measured DI as a firm progresses toward bankruptcy. To do so, we merge the data on bankruptcy filings by publicly traded firms collected by Chava and Jarrow (2004) with that in the UCLA-LoPucki bankruptcy database. In Figure 5, we show the 5th, 10th, 25th, 50th, 75th, 90th, and 95th percentiles of the distribution of the distance to insolvency for those firms that end up filing for bankruptcy in the 36 months prior to filing for bankruptcy or being delisted. As one can see, these percentiles decline monotonically as bankruptcy approaches. A year prior to bankruptcy, 90% of these firms have a measured DI that is below the cutoff of 3 for investment grade, and 50% are near the cutoff of 1 for being highly vulnerable. At bankruptcy, all firms have a measured DI below 2, associated with being vulnerable, and nearly all firms have a measured DI below 1, associated with being highly vulnerable.

Next, we consider the relationship between the distribution of measured DI and aggregate default rates. We use Exhibit 30 in Moody's (2012), which documents annual issuer-weighted corporate default rates for all rated corporations. For comparability, we construct an annual series of measured DI by computing firm-level volatilities over an annual window. In Figure 6, we plot the fraction of firms with measured DI less than 1, against Moody's aggregate default rate series. The figure reveals that the two series are highly correlated, with a correlation of 0.82. Even if we use the fraction of firms with annual measured DI less than 2, the correlation of this fraction with Moody's annual

<sup>&</sup>lt;sup>26</sup>See Bharath and Shumway (2008) for a systematic empirical comparison of structural and nonstructural models of default prediction. There is a large debate in the default prediction literature on the relative benefits of structural vs. non-structural approaches. The recent evidence in Schaefer and Strebulaev (2008) suggests that structural models capture credit risk well, and that any remaining mispricing is likely due to non-credit factors such as bond market illiquidity.

default rates is 0.72. Thus, we conclude that the fraction of firms with low measured DI is highly correlated with realized annual default rates.

## 4 Financial Soundness, 1926–2012

We now use our measure of DI to retrace the history of U.S. firms' financial soundness, from 1926 to the present. Our interest is to characterize the evolution of the cross-sectional distribution of measured DI across firms at a monthly frequency over this time period. We first show that this distribution is approximately lognormal each month from 1926 to 2012 and hence can be characterized by two if its moments.<sup>27</sup> We next show that most of the movements in this distribution are accounted for by changes in the cross-sectional mean (and median) of log measured DI rather than by changes in its cross-sectional dispersion. We then define episodes that we term *insolvency crises* in terms of movements in the distribution of distance to insolvency across firms and examine our three empirical questions regarding the relationship between insolvency crises and business cycles over this long historical time period.

#### 4.1 A Lognormal Approximation

To analyze the distribution of measured DI across firms in a simple way, we first argue that, empirically, in the cross section, the log of measured DI is approximately normally distributed.<sup>28</sup> Formally, consider the following empirical diagnostic for a lognormal distribution, in the spirit of the Kolmogorov Smirnov specification test. We consider the transformed variable

$$N\left(\frac{\log\left(DI_{t}\right) - \mathrm{mean}_{t}}{\mathrm{standard\ deviation}_{t}}\right) \tag{3}$$

where  $N(\cdot)$  is the cumulative distribution of a standard normal distribution. If measured DI were truly lognormal in the cross section, then the transformed variable (3) should be uniform, implying that its percentiles should be exactly equal to 0.5, 0.25, 0.5, 0.75, 0.90, and 0.95 in each month. Figure 7 shows that this is approximately true: it plots

<sup>&</sup>lt;sup>27</sup>See Kelly, Lustig, and Van Nieuwerburgh (2012), which studies the factor structure of individual firm volatilities, and who were the first to our knowledge to establish the approximate lognormality of the distribution of firm level volatilities. In contemporaneous work, Kelly, Lustig, and Van Nieuwerburgh (2013b) study the evolution of the cross section distribution of volatility and relate this distribution to the firm size distribution in a spatial network model.

<sup>&</sup>lt;sup>28</sup>Figure S5 in the supplementary appendix shows the evolution over time of percentiles of the cross section distribution of DI. It is clear that the distribution of measured DI appears to fan out at high levels: the higher percentiles cutoffs are further apart than the lower ones, so it is intuitive that taking logs would make the percentile cutoffs more evenly distributed.

the empirical percentile cutoffs of the transformed random variable (3) for each month 1926–2012, and shows that they do not deviate much from their theoretical values. We thus conclude that measured DI is approximately lognormal in the cross section each month. This is convenient for summarizing the data, since we can then approximately characterize the entire distribution each month with its mean or median and standard deviation.

Figure 8 plots the time series of the cross-sectional mean and standard deviation of log measured DI. One sees that there are some fluctuations in the standard deviation over time, notably as stocks from new exchanges are added to CRSP in July 1962, December 1972, and March 2006. However, these fluctuations are much smaller than those of the mean. This suggests that time variations of the cross-sectional mean of log measured DI account for most of the time variations of the entire cross-sectional distribution.

#### 4.2 Insolvency Crises and Recessions

From now on we study time variation in one moment of the measured DI distribution: the median. We use our calibration to focus on one particular cutoff for median measured DI and define a *deep* insolvency crisis as one in which the median measured DI falls below 1. In deep crises, half of publicly traded firms have a measured DI associated with a highly vulnerable credit rating.

Although we point to particular dates as insolvency crises based on this calibrated cutoff, the entire time series of the median measured DI can also be used as a continuous measure of the financial soundness of all U.S. firms. This complements indicator measures of financial crises such as that in Schularik and Taylor (2012), which dates financial crises based on both qualitative and quantitative data.<sup>29</sup> The median is also a useful summary statistic for the entire distribution. Indeed, recall that log measured DI is approximately lognormal, so the log of median is approximately equal to the mean of log. Moreover, we established that the cross-sectional standard deviation fluctuates much less than the mean over time. Thus, in a deep insolvency crisis, the large negative shift in median measured DI is associated with approximately parallel negative shifts, in a log scale, of all other percentiles of measured DI.

To assess the size of these negative shifts, consider the following calculation. In a deep crisis, log measured DI is approximately normally distributed, with a cross-sectional mean equal to zero, the log of the median, and a standard deviation that is roughly equal to 0.61 (1.8 in levels), its historical average. Hence, during a deep crisis about  $N\left(\frac{\log 3}{0.61}\right) \simeq 96\%$ of publicly traded firms have a measured DI below 3 associated with speculative grade

<sup>&</sup>lt;sup>29</sup>Jordà, Schularik, and Taylor (2011), Jordà, Schularik, and Taylor (2012), and others use such measures to examine the role of financial crises in aggregate fluctuations.

rating, and about  $N\left(\frac{\log 2}{0.61}\right) \simeq 87\%$  of publicly traded firms have a measured DI below 2 associated with a vulnerable credit rating. Hence, deep financial crises are also broad.<sup>30</sup>

Figure 9 plots the median measured DI over time against a log scale and shows the *deep insolvency crises* that occurred in October of 1929 and the Great Depression, the fall of 1937, and the fall of 2008. During these times, 50% of firms became highly vulnerable, with a measured DI below 1. Thus, in relation to business cycles over this time period, the worst recessions (the Great Depression and the Great Recession) coincide with deep insolvency crises. One can also see in Figure S6 in the supplementary appendix that, in the 1932–1933 and 2008 insolvency crises, 95% of firms had a measured DI below 2, well below the cutoff of 3 for investment grade. Thus, these crises are even broader than suggested by the lognormal approximation with constant cross-sectional standard deviation.

This finding that the recessions of 1932–1933, 1937, and 2008 are distinctive in being associated with insolvency crises is not particularly sensitive to the thresholds used to define insolvency crises. In the other recessions marked in Figure 9, median measured DI fell a bit below 2 only in the recessions of the early and mid 1970's and in the 2001 recession.

In this paper so far, we measure the cross section distribution of the financial soundness of firms using market signals gathered from the public *equity markets*. There is also a large literature in macroeconomics that uses movements in indices of credit spreads in *bond markets* as a proxy for financial conditions impacting firms' financial soundness.<sup>31</sup> Conceptually, within the context of a structural credit risk model such as the Leland model, a firm's equity volatility and bond spreads should both be signals of that firm's unobserved underlying distance to insolvency, and hence, we should see that indices of bond spreads rises markedly in the same insolvency crises that we identify with our equitybased measure of the cross section distribution of firms' distance to insolvency.<sup>32</sup>

We find this to be the case. We have already shown the close correspondence of measured DI and bond spreads for the period 1997-2012 using indices of option-adjusted bond spreads constructed by the Bank of America-Merrill Lynch. We now consider the

<sup>&</sup>lt;sup>30</sup>To confirm this approximate calculation, Figure S6 in the supplementary appendix shows the true 95th percentile of log measured DI (in red) versus an approximate 95th percentile, calculated assuming that the log of measured DI is normally distributed with a *constant* standard deviation, equal to the 1926–2012 average. The 95th percentile of a lognormal distribution is equal to  $mean_t + N^{-1}(0.95) \times$ standard deviation<sub>t</sub>, so in principle it could be quite sensitive to fluctuations in standard deviation. One sees, however, that, empirically, most variations of the 95th percentile are accounted for by variations of the mean.

<sup>&</sup>lt;sup>31</sup>See, for example, Bernanke, Gertler, and Gilchrist (1999) and, more recently, Gilchrist and Zakrajšek (2012)

<sup>&</sup>lt;sup>32</sup>In related work, Gilchrist, Sim, and Zakrajsek (2010) find a close correspondence between firm-specific equity volatility and firm-specific bond spreads over the full 1963 to 2009 time period.

correlation between median measured DI and two other indices of bond spreads that cover a longer time period. One index of bond spreads that we consider is the index of optionadjusted spreads constructed by Gilchrist and Zakrajšek (2012) (GZ spread) covering the period 1973-2010.<sup>33</sup> The other index that we consider is the spread between the index of yields on Baa corporate bonds constructed by Moody's and the yield on long-term government debt covering the period 1926-2012.<sup>34</sup>

Given the linear relationship between the log of corporate bond spreads and the log of inverse equity volatility observed in Figure 3, we compare the level of these spreads to the level of equity volatility for the median firm in the cross section each month over the 1926 through 2012 time period. We show this comparison between our equity-based measure of the distribution of financial soundness across firms and these indices of corporate bond spreads in Figure 10. The Moody's Baa bond spread and the GZ spread are both plotted using the scale on the left vertical axis (in percentage points). The annualized equity volatility of the median firm each month is plotted using the scale on the right vertical axis (again in percentage points).

In this figure, we see a close correspondence between our equity based measure of the distribution of financial soundness across firms and these indices of bond spreads in the period 1926 to 1941 and again from 2000 through at least 2010. In particular, the three episodes that we identified as insolvency crises associated with large recessions (episodes in which the equity volatility of the median firm exceeds 100%) are also periods with very elevated bond spreads. We see these data as confirming our main finding that there are three large insolvency crises over the period 1926-2012 associated with three large recessions.

It is noteworthy that there are several episodes in which equity volatility spikes upward markedly but bond spreads do not. These episodes include October 1929, September 1946, October 1987, and October 1998. These episodes are also distinguished by the fact that these spikes in equity volatility do not correspond to recessions. One potential interpretation of these episodes worth pursuing in future research is based on the persistence of movements in equity volatility. In principle, in the context of a Leland-type structural credit risk model, longer-term bond spreads should reflect market participants' perceptions of firms' asset volatility over a longer-term horizon. Our equity-based measure of firms' financial soundness based on realized volatility can spike up due to a few large movements in stock prices over a few days. But if market participants do not perceive

 $<sup>^{33}\</sup>mathrm{The}$  data for this GZ spread is available on the AEA website.

<sup>&</sup>lt;sup>34</sup>We collect the data from the FRED website at the St. Louis Federal Reserve Bank. We take the difference between the Moody's Seasoned Baa Corporate Bank yield monthly 1926-2012 and the 10 year constant maturity Treasury rate monthly 1962-2012 or the yield on Long-Term U.S. Government Securities monthly 1926-1961.

that this elevated volatility will persist, they do not price it into bond spreads. Under this interpretation, our equity-based measure when computed using realized volatility over a one-month horizon may be subject to important measurement errors if movements in realized volatility are very transient.<sup>35</sup>

The correspondence between equity volatility and bond spreads is much less tight in the period 1941 to 2000. Both bond spreads and median equity volatility are low during this time period (in a long historical perspective). Part of the difficulty here may be a problem of composition — the universe of firms issuing bonds included in these bond spread indices during this time period may be quite different than the universe of firms with publicly traded equity. As evidence in favor of the hypothesis that composition problems are impacting the bond data, consider the substantial differences between the Moody's Baa spread and the GZ spread over the period 1973 to 2001 that then largely disappear after 2001 when the bond market became broader.

We see two reasons that our use of equity data to measure the distribution of financial soundness across firms adds to measurement over and above what can be done with bond spreads. First, by using equity data, we can measure changes in the financial soundness of firms that do not have long term debt (bonds or bank debt) during insolvency crises (which are also periods of elevated bond spreads). Data on such firms, which we briefly discuss below as well as in supplementary appendix E, helps shed light on the question of whether it is frictions in credit markets themselves that are leading to these signals of financial distress among firms or issues centered on the financial soundness of the firms themselves. Second, using our structural model, we can decompose the observed movements in equity volatility (and correlated bond spreads) into components due to changes in leverage, changes in a common or aggregate component of business risk, and changes in the variance of firm-specific or idiosyncratic business risk. We examine these questions in the next section.

#### 4.3 Leverage versus Asset Volatility

Given the definition of leverage adjusted for asset volatility in our simple structural model and the relationship of this concept to DI, an insolvency crisis can occur for two reasons: one due to an increase in leverage (a drop in the equity cushion,  $\frac{V_{At}-V_{Bt}}{V_{At}}$ ) and the other due to an increase in asset volatility (an increase in business risk,  $\sigma_{At}$ ). In this section, we

<sup>&</sup>lt;sup>35</sup>Schwert (1990) studies equity volatility over the 1987 crash. Using S&P500 index option prices along with the Merton (1974) model, he concludes that market participants expected the volatility spike to be short lived. There is a considerable literature that looks to model the dynamics of equity volatility econometrically. See, for example Bekaert et al. (2012). We have chosen not to do so here because we do not wish to impose a parametric structure on the dynamics of equity volatility at this point in our analysis.

decompose DI into its leverage and asset volatility components to study the contribution of each to the level of DI over time. We provide evidence that the contribution of changes in asset volatility to movements in the distribution of DI across firms is substantially more important than the contribution of leverage. We also document that the changes in equity volatility that we observe are mainly due to changes in the volatility of idiosyncratic innovations to firms' equity values rather than changes in common or aggregate innovations to equity values.

To decompose movements in the distribution of DI across firms into components due to changes in leverage and changes in asset volatility, we take advantage of our previous finding that most of the movements in the cross section distribution of DI across firms can be summarized by movements in the mean of this distribution. If we use the mean of the distribution of the log of DI across firms as a summary statistic for the position of the entire cross section distribution, then we can decompose these movements in the mean of the log of DI into movements in the mean of the log of leverage and movements in the mean of the log of asset volatility.<sup>36</sup>

We analyze here the simple unlimited liability benchmark. In appendix B, we show that the results do not change substantially if one calculates asset values and volatilities under limited liability, using an option adjustment based on Black and Scholes' model. Under unlimited liability,  $V_{At} = V_{Et} + V_{Bt}$ , and thus we can decompose log DI into leverage and asset volatility simply using

$$\log\left(\frac{1}{\sigma_{Et}}\right) = \log\left(\frac{V_{At} - V_{Bt}}{V_{At}}\right) + \log\left(\frac{1}{\sigma_{At}}\right). \tag{4}$$

We use quarterly COMPUSTAT data on total liabilities interpolated to daily data as an estimate of  $V_{Bt}$ , and we use daily equity values to compute  $V_{Et}$ . Note that although our estimate of  $V_{Bt}$  based on book values might be slow moving, our estimate of leverage moves on a daily basis due to fluctuations in  $V_{Et}$ . We compute for each firm, monthly asset volatility using the daily data for firm value  $V_{Et} + V_{Bt}$  for the days within the month. Figure 11 plots the mean log distance to insolvency and asset volatility terms in equation (4), for the 1972–2012 time period. Clearly, most of the changes in the level of DI are due to changes in the level of asset volatility, especially in more recent data.

To show more clearly the relative contribution of leverage and asset volatility, Figure 12 calculates a counterfactual time series by shifting the median  $\log(1/\sigma_E)$  up by a constant, so that it has the same historical mean as the median  $\log(1/\sigma_A)$ , thus obtaining a "constant leverage" measure of  $\log(1/\sigma_E)$ . The figure strongly suggests that most of

 $<sup>^{36}</sup>$ This result greatly simplifies our analysis relative to the analysis in Choi and Richardson (2013) which focuses on modeling the dynamics of equity volatility for individual firms.

the variation in DI is accounted for by variation in asset volatility. Of particular interest is the role of leverage versus asset volatility in the insolvency crisis of 2008. Figure 12 shows that this crisis was almost entirely due to an increase in asset volatility. This is in contrast to common narratives in the financial press and academic literature, which emphasize the role of an increase in leverage due to a fall in asset values in driving the deterioration in financial soundness in 2008.<sup>37</sup>

As a second piece of evidence of the major contributing role of asset volatility over leverage in determining firms' financial soundness in 2008, we use the decomposition under unlimited liability to compare the percentiles of the cross-sectional distribution of DI in October 2008 with the cross-sectional distribution of DI in October 2008 that would have occurred if leverage for each firm had remained at its level from October 2007 and only asset volatility had risen to its level in October 2008. These percentiles are shown in Figure 13. The first column of colored bars shows the 5th, 10th, 25th, 50th, 75th, 90th, and 95th percentiles of the cross-sectional distribution of DI in October 2007. The second column of colored bars shows the 5th, 10th, 25th, 50th, 75th, 90th, and 95th percentiles of the cross-sectional distribution of DI in October 2008. The third column of colored bars shows the 5th, 10th, 25th, 50th, 75th, 90th, and 95th percentiles of the cross-sectional distribution of DI computed firm-by-firm using that firm's leverage in October 2007 and its asset volatility in October 2008. As is clear in the figure, the percentiles of this counterfactual cross-sectional distribution shown in the third column are quite similar to those found for the actual distribution in October 2008 (shown in the second column) and quite different from those found for the cross-sectional distribution in October 2007 (shown in the first column). Thus, this cross-sectional decomposition provides further evidence that the collapse in the distribution of DI in the fall of 2008 is, in an accounting sense, primarily due to an increase in asset volatility rather than an increase in leverage.

Finally, in supplementary appendix E, we compare the median DI for firms with and without long-term debt. The analysis shows that variation in median DI are similar for the two groups. This supports our view that asset volatility accounts for most of the movements in DI.

We now turn to an examination of the relative magnitude of changes in the volatility of the common, or aggregate component, of firms' equity returns versus changes in the median of the volatility of the idiosyncratic component in firms' equity returns in accounting for movements in the median of the distribution of firms' DI as measured by

<sup>&</sup>lt;sup>37</sup>One may wonder whether these decomposition results are biased by our assumption of unlimited liability. To address this concern, in supplementary appendix B we calculate an option-adjusted asset volatility computed using Black and Scholes' model and compare it to the asset volatility computed using the unlimited liability model. Figure S7 plots the results: as it is clear, the option adjustment does not substantially alter our decomposition.

the (inverse of) the total volatility of their equity returns.<sup>38</sup>

To do this decomposition, first, every month, we regress the daily returns on each stock in CRSP on the daily returns for the equally weighted portfolio and compute the volatility of the idiosyncratic component of that firm's equity returns as the volatility over the month of the daily residuals from this regression.<sup>39</sup> This regression has the form

$$r_{itk} = \alpha_{it} + \beta_{it} r_{EWtk} + \varepsilon_{itk}$$

where the subscript *i* denotes a firm and *k* denotes the day within the month *t*, the subscript *EW* denotes the equally weighted portfolio in CRSP, and the coefficients  $\alpha_{it}$  and  $\beta_{it}$  are estimated separately for every firm *i* and every month *t*. We let  $\sigma_{iTt}$  denote our measure of the volatility in month *t* of the daily total returns  $r_{itk}$  for firm *i* in month *t* and let  $\sigma_{iIt}$  denote our measure of the volatility in month *t* of the daily total returns  $r_{itk}$  for firm *i* in month *t* for firm *i* in month *t*.

To illustrate the importance of movements in the distribution of the volatility of the idiosyncratic component of firm's equity returns  $\sigma_{iIt}$  in accounting for movements in median DI measure as the median of the inverse of the total volatility of firms' equity returns  $1/\sigma_{iTt}$ , in Figure 14, we plot median DI computed using the total volatility of firms' equity returns (in blue) and the median of a counterfactual measure of firms' DI computed using only the volatility of the idiosyncratic component of firms' equity returns  $1/\sigma_{iIt}$ . This counterfactual measure of median DI is computed as if the volatility of the common or aggregate component of firms' equity returns was always set equal to zero for all firms. As can be seen clearly in the figure, this counterfactual measure of median DI using  $1/\sigma_{iIt}$  is quite close to our actual measure of median DI over the entire 1926-2012 time period. We interpret this finding as implying that movements in the volatility of the idiosyncratic component of firms' equity returns accounts for the bulk of the movements in the distribution of DI across firms over this entire time period.<sup>40</sup>

<sup>&</sup>lt;sup>38</sup>The decomposition of volatility into an aggregate, industry, and firm-specific component is the focus of Campbell, Lettau, Malkiel, and Xu (2001). Their Figures 2-4 graph this decomposition and show the importance of firm-specific volatility in overall firm volatility. They also show a substantial correlation between the three volatility series. Kelly, Lustig, and Van Nieuwerburgh (2012) and Bekaert, Hodrick, and Zhang (2012) are more recent examinations of the evolution of the cross section distribution of firms total equity volatility as well as the evolution of the cross section distribution of the volatilities of the idiosyncratic component of firms' equity returns. They examine several proxies for the aggregate component of firms' equity returns including Fama-French factors and a principal components decomposition of returns. We present a simplified version of their procedure.

<sup>&</sup>lt;sup>39</sup>We have repeated this analysis using the three-factors model of Fama and French (1993), and reached identical conclusions.

 $<sup>^{40}</sup>$ For early contributions documenting the relationship between equity market volatility and real activity in the great depression see Officer (1973), who shows that market level volatility was elevated for many years, and Benston (1973), who documents related facts for idiosyncratic volatility as well. Schwert (1989b) and Schwert (1989a) document a link between aggregate real activity and market level volatility

#### 4.4 Financial versus Nonfinancial Firms

A large literature in macroeconomics and finance argues that, when financial intermediaries are financially unsound, they amplify and propagate negative shocks to the real economy. In fact, a commonly held view is that the weak financial soundness of financial intermediaries was the root cause of the large recessions of 1932–1933, 1937, and 2008. A growing literature also argues that changes in regulation and/or the introduction of new financial products changed the risk-taking behavior of financial institutions. Given the prominent role that large financial institutions played in the recent crisis, we focus on the largest financial firms and compare them to their large non-financial peers.

To shed light on the relative financial soundness of large financial versus large nonfinancial firms over time, we compare the distribution of measured DI over time for large financial and large nonfinancial firms.<sup>41</sup> An advantage of our measure is that we do not require accounting or market value information for liabilities, which are hard to measure properly for financial firms. Like any market-based measure, however, our measure of DI based on equity volatilities is influenced by the presence (implicit or explicit) of government subsidies.<sup>42</sup> We also acknowledge that the use of market-based signals for regulation is subject to the usual caveats regarding adverse feedback loops between agents' actions and market prices.<sup>43</sup>

We begin by classifying financial firms as those firms in CRSP with an Standard Industrial Classification (SIC) code in the range of 6000–6999, and comparing the median measured DI for financial firms and non-financial firms. We measure the DI of these financial firms in exactly the same way as we do for all firms.

Figure 15 plots the median measured DI for the 50 largest financial and nonfinancial firms by market capitalization from 1962 to 2012, the period for which there are enough large firms of each type. The main message from this graph is that the median financial soundness of large financial and large nonfinancial firms was quite similar over this time period. From the evidence in Figure 15, it seems hard to argue that changes in bank regulation or financial innovations over the 1962-2007 time period led large financial firms to add leverage relative to their business risk in a manner different from their large

over a long US time series. Schwert (1989b) also argues that changes in aggregate leverage explain a relatively small part of overall market volatility. These two studies differ from ours because because they only study market level volatility and because their focus is the relationship between the volatility of aggregate macroeconomic time series such as inflation and industrial production with overall equity market volatility.

<sup>&</sup>lt;sup>41</sup>See Giammarino, Schwartz, and Zechner (1989) for an early contribution using a structural model of default to consider market-implied valuations of bank assets and the value of deposit insurance.

<sup>&</sup>lt;sup>42</sup>Kelly, Lustig, and Van Nieuwerburgh (2013a) and Lustig and Gandhi (forthcoming) present evidence that government subsidies are evident in bank stock returns and option prices.

<sup>&</sup>lt;sup>43</sup>See Bond, Goldstein, and Prescott (2010), which provides an equilibrium analysis of the use of market signals in regulation.

nonfinancial peers.

One challenge in interpreting this graph is that many firms with SIC codes from 6000 to 6999 are not banks, or at least the type of financial firms frequently discussed in the context of the most recent financial crisis (firms in these SIC codes include health insurers, property firms such as Public Storage, and, most recently, ETFs.) We address this challenge next by studying a set of firms that we call *government-backed large financial institutions*, or GBLFIs. This set of institutions comprises the 18 bank holding companies that currently participate in the Federal Reserve's annual stress tests and eight large financial institutions that failed during the crisis (AIG, Bear Stearns, Fannie Mae, Freddie Mac, Lehman, Merrill Lynch, Wachovia, and Washington Mutual). The full list of GBLFIs together with the dates for which data on their equity returns are available, is provided in Table 1.

Figure 16 plots the median measured DI for the GBLFIs and the 50 largest nonfinancial firms by market capitalization from 1962 to 2012. Again, there does not seem to be evidence in market prices of increased risk taking by the GBLFIs relative to non-financial firms over the period July 1962–July 2007. Thus, again it seems hard to argue that changes in bank regulation or financial innovations over the 1962-2007 time period led these large financial firms to add leverage relative to their business risk in a manner different from their large nonfinancial peers. However, it does appear that the distance to insolvency for the GBLFIs deteriorated relative to their nonfinancial peers starting in August of 2007 and fell to an extremely low level in the depth of the crisis from October 2008 to March 2009. Thus it appears that these firms suffered a sharper deterioration in the financial soundness in the crisis than did their large non-financial peers. Moreover, these firms have been slower to recover their DI since that time. Unfortunately, we cannot readily conduct a similar analysis for the Great Depression because the largest banks at that time were not traded on exchanges and thus are not in the CRSP database of daily returns.

One goal of financial regulation is to identify relatively weak financial institutions in the cross section either before a crisis begins or during the crisis. We are skeptical that regulators can achieve this goal because we find that most of the movements of measured DI, even for the GBLFIs are systemic in nature — measured DI for all of these institutions moves closely together. Figure 17 plots the 90th, 50th, and 10th percentiles of the distribution of measured DI for the GBLFIs. The figure presents clear evidence that the cross-sectional variation in measured DI for these GBLFIs in any given month is quite small relative to the movement in the distribution of DI over time: during this time period, the risk that any one GBLFI is unsound compared with the others is small relative to the risk that the whole group of GBLFIs becomes unsound together. This pattern is particularly apparent in the fall of 2011: these figures indicate that the whole group of GBLFIs was nearly as unsound at that time as the group was in early 2008 or mid-2009.

## 5 Conclusion

This paper is intended as a contribution to measurement: we propose a simple and transparent method for measuring the financial soundness of firms that can be broadly applied to all publicly traded firms in the economy.

We identify three recessions in which a macroeconomic downturn coincides with or follows shortly after a substantial insolvency crisis: 1932–1933, 1937, and 2008. We find that the other recessions in this time period are not associated with significant deteriorations or insolvency crises. Of course, since our findings uncover only a correlation (or lack thereof) between insolvency crises and recession, they do not establish causation. We do, however, see our findings as consistent with the hypothesis that financial frictions may have played a significant role in the recessions of 1932–1933, 1937, and 2008, and that financial frictions (as envisioned by current theories) did not play a significant role in other recessions during this time period. We hope that our research will provoke more detailed studies of the differences between these three recessions and other recessions to see if a stronger empirical and theoretical basis for causal links between financial frictions and the evolution of the macroeconomy can be developed.

A decomposition of our distance to insolvency measure into its leverage and asset volatility components attributes most of the 2008 insolvency crisis to an increase in asset volatility, or business risk. Moreover, we find that the majority of the movement in the distribution of volatilities across firms is due to movement in the distribution of the volatility of the idiosyncratic component of fluctuations in firms' value. Distortions to managerial and equity holder decisions occur when the likelihood of insolvency is high for either reason. Thus, considering only the effects of leverage on agency costs may leave out quantitatively important variation due to time-varying asset volatility. We see this question as being of first-order importance for future research in order to understand the sources of these large changes in asset volatility.

We also find little or no evidence that the evolution of financial soundness across large financial firms differs meaningfully from that of large non-financial firms in the period 1962-2007. This finding casts doubt on the hypothesis that the market perceived that changes in financial regulation and financial innovation played an important role in shaping large financial firms' leverage and risk taking in advance of the most recent crisis relative to the choices made by their large non-financial peers. Finally, we find it distressing that government-backed large financial institutions continued to appear weak in terms of their financial soundness long after the summer of 2007, in spite of the heightened regulatory scrutiny they received following the 2008 financial crisis. Why these firms continued to look financially weak relative to their peers for so long is an open question that calls for further research.



### Time

Figure 1: The value of equity as a function of the value of assets.



Figure 2: The value of equity as a function of the value of assets.



Figure 3: A scatter plot of monthly measured DI versus monthly averages of optionadjusted spreads for the Bank of America-Merrill Lynch corporate bond indices by ratings class for January 1997–December 2012, in log scale. Each point represents a single month and data for one of seven ratings from AAA to CCC and below. Pre–August 2007 data points are blue triangles, and post–August 2007 data points are red circles.



**Figure 4:** A scatter plot of monthly measured DI vs. monthly of averages of 5 year single name CDS rates for 2001–2011, in log scale. Data is pooled by credit rating. Each point represents a single month and one of seven ratings classes from AAA to CCC and below. Pre–August 2007 data points are blue triangles, and post–August 2007 data points are red circles.



Figure 5: The distribution of measured DI for firms that declare bankruptcy in the 60 months prior to bankruptcy or delisting.



**Figure 6:** Annual measured DI versus annual issuer-weighted corporate default rates from Moody's Investor Service Annual Default Study 2012.



Figure 7: The y-axis plots the percentiles of a true lognormal distribution for  $DI_t = 1/\sigma_{Et}$  with the estimated cross-sectional mean and standard deviation for each month, 1926–2012. The colored lines display the empirical percentile cutoffs on each date.



**Figure 8:** The mean and standard deviation of log measured DI, 1926–2012. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.



**Figure 9:** Deep and Broad Insolvency Crises: The log of the median measured DI, 1926-2012. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale. Recessions are indicated by vertical gray bars. The median measured DI hits 1, associated with a highly vulnerable rating, in the Great Depression, 1937, 1987, and the Financial Crisis of 2008.



**Figure 10:** Bond Spread Indices and Median Equity Volatility: The Gilchrist-Zakrajsek bond spread index 1973-2010 (in orange) and the Moody's Baa - long term government debt spread index 1926-2012 (in red) in percentage points are plotted on the left axis. The level of equity volatility for the median firm in the cross section every month 1926-2012 is plotted in percentage points on the right axis.



Figure 11: Leverage and asset volatility under the assumption of unlimited liability, 1971-2012. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.



Figure 12: Measured DI versus constant leverage measured DI, under the assumption of unlimited liability, 1971-2012. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.



Figure 13: The percentiles of measured DI for all firms in October 2007 and October 2008 together with the counterfactual alternative percentiles of DI that would have arisen from October 2007 leverage and October 2008 asset volatility.



Figure 14: Median DI measured using firms' total equity volatility and Median DI using firms' idiosyncratic equity volatility. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.



Figure 15: A comparison of the log median measured DI for the largest 50 financial and non-financial firms in terms of market capitalization, 1962-2012. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.



**Figure 16:** A comparison of the log median measured DI for the Government Backed Large Financial Institutions and the largest 50 non-financial firms in terms of market capitalization, 1962-2012. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.



Figure 17: The 90th percentile, median, and 10th percentile of measured DI for the GBLFI's from 1997-2012. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.



**Figure 18:** The mean of the log of inverse realized versus option implied volatilities, 1993-2012. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.

## References

- Heitor Almeida and Thomas Philippon. The risk-adjusted cost of financial distress. The Journal of Finance, 62:2557–2586, 2007.
- Cristina Arellano, Yan Bai, and Patrick Kehoe. Financial markets and fluctuations in uncertainty. Working paper, March 2011.
- Robert J. Barro. Rare disasters and asset markets in the twentieth century. *Quarterly Journal of Economics*, 121:823–866, 2006.
- Geert Bekaert, Robert J. Hodrick, and Xiaoyan Zhang. Aggregate idiosyncratic volatility. *Journal of Financial and Quantitative Analysis*, 47(6):1155–1185, December 2012.
- George T. Benston. Required disclosure and the stock market: An evaluation of the securities exchange act of 1934. *American Economic Review*, 63:132–155, 1973.
- Ben Bernanke. Nonmonetary effects of the financial crisis in the propagation of the great depression. *The* American Economic Review, 73(3):257–276, 1983.
- Ben Bernanke and Mark Gertler. Agency costs, net worth, and business fluctuations. *The American Economic Review*, 1:14–31, 1989.
- Ben Bernanke, Mark Gertler, and Simon Gilchrist. The financial accelerator in a quantitative business cycle framework. In John Taylor and Michael Woodford, editors, *Handbook of Macroeconomics*, chapter 21, pages 1341–1392. Elsevier, 1999.
- Harjoat S. Bhamra, Lars-Alexander Kuehn, and Ilya A. Strebulaev. The aggregate dynamics of capital structure and macroeconomic risk. *The Review of Financial Studies*, 23:1–55, 2010.
- Sreedhar Bharath and Tyler Shumway. Forecasting default with the merton distance to default model. *Review of Financial Studies*, 21(3):1339–1369, May 2008.
- Fischer Black and John C. Cox. Valuing corporate securities: Some effects of bond indenture provisions. Journal of Finance, 31(2):351–367, May 1976.
- Fischer Black and Myron Scholes. The pricing of options and corporate liabilities. Journal of Political Economy, 81:637–654, 1973.
- Nicholas Bloom. The impact of uncertainty shocks. *Econometrica*, 77(3):623–685, May 2009.
- Nicholas Bloom, Max Floetotto, Nir Jaimovich, Itay Saporta, and Stephen Terry. Really uncertain business cycles. 2013.
- Phillip Bond, Itay Goldstein, and Edward S. Prescott. Market based corrective actions. Review of Financial Studies, 23:781–820, 2010.
- Markus K. Brunnermeier and Yuliy Sannikov. A macroeconomic model with a financial sector. Working paper, Princeton University, 2012.
- John Y. Campbell, Martin Lettau, Burton G. Malkiel, and Yexiao Xu. Have individual stocks become more volatile? an empirical exploration of idiosyncratic risk. The Journal of Finance, 56:1–43, 2001.
- J.Y. Campbell and G.B. Taksler. Equity volatility and corporate bond yields. *Journal of Finance*, 58(9): 2321–2350, December 2003.
- J.Y. Campbell, J. Hilscher, and J. Szilagyi. In search of distress risk. Journal of Finance, 63(6):2899–2939, December 2008.
- Charles T. Carlstrom and Timothy S. Fuerst. Agency costs, net worth, and business fluctuations: A computable general equilibrium analysis. *The American Economic Review*, 87:893–910, 1997.

- Sudheer Chava and Robert A. Jarrow. Bankruptcy prediction with industry effects. *Review of Finance*, 8(4):537–569, 2004.
- Hui Chen. Macroeconomic conditions and the puzzles of credit spreads and capital structure. *The Journal* of *Finance*, 65:2171–2212, 2010.
- Long Chen, Pierre Collin-Dufresne, and Robert S. Goldstein. On the relation between the credit spread puzzle and the equity premium puzzle. *Review of Financial Studies*, 22:3367–3409, 2009.
- Jaewon Choi and Matthew Richardson. The volatility of the firm's assets. Working Paper, 2013.
- Lawrence Christiano, Roberto Motto, and Massimo Rostagno. Financial factors in economic fluctuations. Working paper, May 2010.
- Thomas Cooley and Vincenzo Quadrini. Financial markets and firm dynamics. *The American Economic Review*, 91(5):1286–1310, 2001.
- Thomas Cooley, Ramon Marimon, and Vincenzo Quadrini. Aggregate consequences of limited contract enforceability. *Journal of Political Economy*, 112(4):817–847, 2004.
- Francisco Covas and Wouter J. Den Haan. The role of debt and equity finance over the business cycle. Working Paper, 2011.
- Vasco Cúrdia and Michael Woodford. Credit frictions and optimal monetary policy. BIS Working Papers, 278, 2009.
- Douglas Diamond and Zhiguo He. A theory of debt maturity: The long and short of debt overhang. *The Journal of Finance*, forthcoming.
- Darrell Duffie. Measuring Corporate Default Risk. Oxford University Press, 2011.
- Darrell Duffie, Leandro Saita, and Ke Wang. Multi-period corporate default prediction with stochastic covariates. Journal of Financial Economics, 83:635–665, 2007.
- Darrell Duffie, Andreas Eckner, Guillaume Horel, and Leandro Saita. Frailty correlated default. *Journal* of Finance, 64(5):2089–2123, October 2009.
- Eugene F. Fama and Kenneth R. French. Common risk factors in the returns on stock and bonds. Journal of Financial Economics, 33:131–156, 1993.
- Vladimir Finkelstein, Jean-Pierre Lardy, George Pan, and Thomas Ta. Credit grades technical document. *Risk Metrics Group*, 2002.
- Xavier Gabaix. Variable rare disasters: An exactly solved framework for ten puzzles in macro-finance. Quarterly Journal of Economics, 127(2):645–700, 2012.
- Mark Gertler and Peter Karadi. A model of unconventional monetary policy. *Journal of Monetary Economics*, 58:17–34, 2011.
- Mark Gertler and Nobuhiro Kiyotaki. Financial intermediation and credit policy in business cycle analysis. In *Handbook of Monetary Economics*, volume 3, chapter 11, pages 547–599. Elsevier, 2010.
- Ronald Giammarino, Eduardo Schwartz, and Josef Zechner. Market valuation of bank assets and deposit insurance and canada. The Canadian Journal of Economics, 22(1):109–127, February 1989.
- Kay Giesecke, Francis A. Longstaff, Stephen Schaefer, and Ilya Strebulaev. Corporate default risk: A 150 year perspective. Journal of Financial Economics, 102:233–250, 2011.
- Simon Gilchrist and Egon Zakrajsek. Credit spreads and business cycle fluctuations. American Economic Review, 2012:1692–1720, 2012.

- Simon Gilchrist and Egon Zakrajšek. Credit supply shocks and economic activity in a financial accelerator model. In Alan Blinder, Andrew Lo, and Robert Solow, editors, *Rethinking the Financial Crisis*. Russell Sage Foundation, 2012.
- Simon Gilchrist, Jae W. Sim, and Egon Zakrajsek. Uncertainty, financial frictions, and investment dynamics. Working paper, 2010.
- Joao Gomes and Lukas Schmid. Equilibrium credit spreads and the macroeconomy. *Working Paper*, 2010.
- Francois Gourio. Disaster risk and business cycles. American Economic Review, Forthcoming.
- Dirk Hackbarth, Jianjun Miao, and Erwan Morellec. Capital structure, credit risk and macroeconomic conditions. Journal of Financial Economics, 82:519–550, 2006.
- Zhiguo He and Arvind Krishnamurthy. Intermediary asset pricing. *American Economic Review*, 103, 2013.
- Urban Jermann and Vincenzo Quadrini. Macroeconomic effects of financial shocks. American Economic Review, 102:238–71, 2012.
- Oscar Jordà, Moritz Schularik, and Alan M. Taylor. Financial crises, credit booms, and external imbalances: 140 years of lessons. *IMF Economic Review*, 59:340–378, 2011.
- Oscar Jordà, Moritz Schularik, and Alan M. Taylor. When credit bites back: Leverage, business cycles, and crises. *NBER Working Paper*, 2011-27, 2012.
- Kyle Jurado, Sydney C. Ludvigson, and Serena Ng. Measuring uncertainty. 2013.
- Aubik Kahn and Julia Thomas. Credit shocks and aggregate fluctuations in an economy with production heterogeneity. *Journal of Political Economy*, Forthcoming.
- Brian Kelly, Hanno Lustig, and Stijn Van Nieuwerburgh. Too-systemic-to-fail: What option markets imply about sector-wide government guarantees. Working paper, Chicago Booth, UCLA, Anderson and NYU Stern, 2013a.
- Bryan Kelly, Hanno Lustig, and Stijn Van Nieuwerburgh. The volatility factor structure. *Working Paper*, 2012.
- Bryan T. Kelly, Hanno Lustig, and Stijn Van Nieuwerburgh. Firm volatility in granular networks. 2013b.
- Charles P. Kindleberger and Robert Aliber. Manias, Panics, and Crashes: A History of Financial Crises. Number 39 in Wiley Investment Classics. John Wiley and Sons, fifth edition, 2005.
- Nobuhiro Kiyotaki and John Moore. Credit cycles. Journal of Political Economy, 105:211–248, 1997.
- Hayne E. Leland. Corporate debt value, bond covenants, and optimal capital structure. Journal of Finance, 49(4):1213–1252, September 1994.
- Francis Longstaff and Eduardo Schwartz. A simple approach to valuing risky fixed and floating rate debt. Journal of Finance, 50(3):789–819, July 1995.
- Hanno Lustig and Priyank Gandhi. Size anomalies in bank stock returns. The Journal of Finance, forthcoming.
- Robert C. Merton. On the pricing of corporate debt: The risk structure of interest rates. Journal of Finance, 29(2):449–470, May 1974.
- Franco Modigliani and Merton H. Miller. The cost of capital, corporate finance and the theory of investment. American Economic Review, 48:262–97, 1958.
- Moody's. Annual default study: Corporate default and recovery rates, 1920-2011. Credit Policy, 2012.

Tyler Muir. Financial crises, risk premia, and the term structure of risky assets. Working Paper, 2013.

- Stuart C. Myers. Determinants of corporate borrowing. *Journal of Financial Economics*, 5:147–175, 1977.
- R. R. Officer. The variability of the market factor of the new york stock exchange. *The Journal of Business*, 46:434–453, 1973.
- Adriano Rampini and S. Viswanathan. Collateral, risk management, and the distribution of debt capacity. Journal of Finance, 65(6):2293–2322, December 2010.
- Adriano Rampini and S. Viswanathan. Financial intermediary capital. Working paper, March 2012.
- Carmen Reinhart and Kenneth Rogoff. This Time Is Different: Eight Centuries of Financial Folly. Princeton University Press, 2009.
- Thomas A. Rietz. The equity risk premium: A solution. Journal of Monetary Economics, 22, 1988.
- Stephen Schaefer and Ilya Strebulaev. Structural models of credit risk are useful: Evidence from hedge ratios on corporate bonds. *Journal of Financial Economics*, 90:1–19, 2008.
- Moritz Schularik and Alan Taylor. Credit booms gone bust: Monetary policy, leverage cycles, and financial crises, 1870-2008. *American Economic Review*, 102:1029–1061, 2012.
- William G. Schwert. Business cycles, financial crises, and stock volatility. Carnegie-Rochester Conference Series on Public Policy, pages 83–126, 1989a.
- William G. Schwert. Why does stock market volatility change over time? The Journal of Finance, 44: 1115–1153, 1989b.
- William G. Schwert. Stock volatility and the crash of '87. Review of Financial Studies, 3:77–102, 1990.
- Zhao Sun, David Munves, and David Hamilton. Public firm expected default frequency (edf) credit measures: Methodology, performance, and model extensions. Moody's Analytics Modeling Methodology, June 2012.
- Robert Townsend. Optimal contracts and competitive markets with costly state verification. Journal of Economic Theory, 22:265–293, 1979.
- Maria Vassalou and Yuhang Xing. Default risk in equity returns. Journal of Finance, 59:831–868, 2004.
- Anne P. Villamil. Modigliani-miller theorem. In The New Palgrave Dictionary of Economics, Second Edition. Eds. Steven N. Durlauf and Lawrence E. Blume. Palgrave Macmillan, 2008.
- Stephen Williamson. Financial intermediation, business failures and real business cycles. Journal of Political Economy, pages 1196–1216, 1987.

# **Appendix For Online Publication**

## A Leland (1994) structural model

Under the true "physical" measure, the value of the firm's assets,  $V_A$ , follows a geometric Brownian motion with drift  $\mu_A$  and volatility  $\sigma_A$ . The firm pays a dividend  $\delta V_A$  per period. Under the risk-neutral measure, the value of the firm's assets follows

$$dV_{At} = (r - \delta)V_{At} dt + \sigma_A V_{At} dB_t^Q$$

The intuition for the risk-neutral drift of  $r - \delta$  is simply that, under the risk-neutral measure, the expected return from buying the assets at  $V_{At}$ , selling at  $V_{At+dt}$ , and receiving the dividend flow  $\delta V_{At} dt$  should be equal to rdt. Assume that the equity holders have to pay c (per unit of time) to the debt holders until either (i) equity holders choose to default or (ii) creditors exercise their right to force equity holders to default, when the value of the assets reach a protective covenant threshold  $V_A^P$ . Let  $\tau_P$  be the first time the asset value falls below the protective covenant threshold,  $V_A^P$ . The problem of the equity holder is to choose a stopping time  $\tau$  in order to solve

$$w(V_A) = \sup_{\tau} \mathbb{E}^Q \left[ \int_0^{\tau \wedge \tau_P} \left( \delta V_{At} - c \right) e^{-rt} dt \right].$$

Consider equity holders starting with two different initial levels of assets,  $V_{A0} < V'_{A0}$ . Clearly, the equity holders starting with  $V'_{A0}$  can always mimic the policy of equity holders and creditors starting at  $V_{A0}$  and would earn a higher payoff, implying that  $w(V_A)$  is nondecreasing. This also shows that an optimal policy is of the threshold form: there is a  $V_A^*$ such that when  $V_A \leq V_A^*$ , equity holders default, or are forced into default by creditors, and continue operating the firm otherwise. Thus, the Bellman equation for the value of equity is

$$V_A \le V_A^* : w(V_A) = 0$$
  
$$V_A \ge V_A^* : rw(V_A) = -c + \delta V_A + w'(V_A)(r - \delta)V_A + w''(V_A)\frac{\sigma_A^2}{2}V_A^2$$

A particular solution to the second-order ordinary differential equation (ODE) is  $V_A - V_B$ , where  $V_B = c/r$ . The general solution of the corresponding homogeneous ODE is of the form  $K_1 V_A^{\phi} + K_2 V_A^{-\theta}$ , where  $K_1$  and  $K_2$  are constant, and  $\phi$  and  $\theta$  are the positive roots

$$\phi^2 \frac{\sigma_A^2}{2} + \phi \left( r - \delta - \frac{\sigma_A^2}{2} \right) - r = 0 \tag{5}$$

$$\theta^2 \frac{\sigma_A^2}{2} - \theta \left( r - \delta - \frac{\sigma_A^2}{2} \right) - r = 0.$$
(6)

When  $V_A \to \infty$ , the value of equity has to asymptote to  $V_A - V_B$ , implying that  $K_1 = 0$ . The constant  $K_2$  is found by value matching  $w(V_A^*) = 0$ , which delivers

$$K_2 = f(V_A^{\star})$$
 where  $f(x) \equiv -(x - V_B) x^{\theta}$ .

The optimal threshold maximizes f(x) subject to  $x \ge V_A^P$ . Differentiating f(x) with respect to x reveals that it is hump shaped and reaches a unique maximum at  $\frac{\theta}{1+\theta}V_B$ . Therefore, the optimal threshold is

$$V_A^{\star} = \max\left\{V_A^P, \frac{\theta}{1+\theta}V_B\right\} \text{ and } w(V_A) = V_A - V_B - \left(V_A^{\star} - V_B\right)\left(\frac{V_A}{V_A^{\star}}\right)^{-\theta}$$

Convexity follows because  $V_A^* \leq V_B$  by our assumption that  $V_A^P \leq V_B$ . Simple calculation shows that  $w'(V_A^*) \geq 0$  and that  $w'(\infty) = 1$ , implying that  $w(V_A)$  is nondecreasing and has a slope less than one.

## **B** Calculating $V_A$ and $\sigma_A$ using Black and Scholes

Following the empirical literature, we can use the Black and Scholes's model to calculate asset values,  $V_A$ , and volatilities,  $\sigma_A$ , using data on equity values and accounting data on liabilities. We use the values of  $V_A$  and  $\sigma_A$  can then be used to calculate an estimate of DI as defined in equation (1), or to calculate Black and Scholes (1973)'s DD, as defined in Section 3.4.

The algorithm. calculate Black and Scholes (1973)'s DD using an iterative algorithm that closely follows Vassalou and Xing (2004) and Duffie (2011). For each publicly traded firm in our sample, we assume that the value of the assets,  $V_A$ , is a geometric Brownian motion with volatility  $\sigma_A$ . We view equity as a call option with an underlying equal to the value of the assets,  $V_A$ , a maturity equal to one year, and a strike price equal to  $V_B$ . Under these assumptions, the Black and Scholes' formula implies that the value of equity

2

of

is given by:

$$V_E = N(d_1)V_A - N(d_2)V_B e^{-r},$$
(7)

where  $N(\cdot)$  is the cumulative distribution function of a standard normal random variable, and

$$d_1 \equiv \frac{\log(V_A) - \log(V_B) + r + \frac{\sigma_A^2}{2}}{\sigma_A}$$
, and  $d_2 = d_1 - \sigma_A$ . (8)

The iterative algorithm. We initialize our iterative algorithm for calculating  $V_A$  and  $\sigma_A$  by setting  $V_A^{(0)} = V_E + V_B$ , where  $V_E$  is the market capitalization of the firm, calculated using the CRSP data on price and number of shares outstanding. Following the literature, we take  $V_B$  to be the the sum of short term liabilities, and half of long-term liabilities, as given in COMPUSTAT. Consistent with Gilchrist and Zakrajsek (2012), for each firm we restrict attention to those times during which quarterly data are available, and we linearly interpolate between points to obtain daily data.

At step n of our algorithm, we have a candidate time series  $V_A^{(n)}$  for the value of the assets on each day of our sample. Given  $V_A^{(n)}$ , we obtain a daily time series for asset realized volatility,  $\sigma_A^{(n)}$ , by computing the annualized square root of the average squared daily returns on the assets during the month. Given  $V_A^{(n)}$  and  $\sigma_A^{(n)}$ , we use equation (8) to calculate a time series for  $d_1^{(n)}$  and  $d_2^{(n)}$ . To deal with firms with small liabilities, we cap  $\log(V_A^{(n)}/V_B)$  at 4 (the results turn out to be largely insensitive to this). In applying the formula, we take the interest rate to be the one-year Treasury constant-maturity (daily frequency) from the Federal Reserve's H.15 report. We then use equation (7) to obtain a new candidate time series for the value of the assets:

$$V_A^{(n+1)} = (1-\omega)V_A^{(n)} + \omega \frac{V_E + N\left(d_2^{(n)}\right)V_B e^{-r}}{N\left(d_1^{(n)}\right)},$$

where  $\omega$  is a relaxation parameter, which we set equal to 0.2 to improve convergence. We terminate our algorithm when the norm of  $(V_A^{(n+1)} - V_A^{(n)})/V_A^{(n)}$  is less than  $10^{-5}$ . Convergence occurs for over 95% of the stocks in the sample.

An estimate of DI. Using the values of  $V_A$  and  $\sigma_A$  implied by Black and Scholes (1973), and the liability  $V_B$  measured as above, one obtains an estimate of DI using equation (1).

**Black and Scholes' DD.** Following the literature, the Black and Scholes' and Merton distance to default is defined as

$$DD \equiv \frac{\log(V_A) - \log(V_B) + \mu_A - \frac{\sigma_A^2}{2}}{\sigma_A},$$

where  $V_A$  and  $\sigma_A$  are calculated using the iterative algorithm described above, and  $\mu_A$  is the mean return on the assets over the time period.

## C DI and Black and Scholes's Distance to Default

In this section we consider the relationship between DI *Black and Scholes' Distance to Default* (DD). A large empirical literature in corporate finance examines the performance of DD as an indicator of the likelihood that a firm will declare bankruptcy and/or default on a bond. Duffie et al. (2009) and Duffie et al. (2007) document the economic importance of distance to default in determining default intensities.<sup>44</sup> Duffie (2011) is an important recent survey of such work. Moody's Analytics produces and sells estimates of the likelihood that publicly traded firms will default on their bonds using a similar methodology (Sun, Munves, and Hamilton, 2012). Campbell et al. (2008) provide further evidence on the role of equity volatility in forecasting firms' financial distress in a reduced form framework.

To calculate DD, we use data on a firm's equity value and volatility, together with accounting data on the firm's liabilities, and we follow a procedure outlined in Duffie (2011) based on Black and Scholes' option pricing formula. See Appendix B for details.<sup>45</sup> In Figure S4 we show a scatter plot of our computed DD against measured DI, monthly from December 1985 to December 2012, for the seven rating classes AAA to CCC and below. While the scale obviously differs, since our DI is measured in levels and DD is measured in logs, the figure shows a clear monotonic relationship between the two. Note, however, that since this relationship is non-linear, one would have to adjust the specification of the bankruptcy or default prediction regressions run in the literature cited above to perform a comparison of the accuracy of our measure of DI in default prediction.

 $<sup>^{44}</sup>$ Duffie et al. (2007) report that a 10% reduction in distance to default causes an estimated 11.3% increase in default intensity, and that distance to default is the most economically important determinant of the term structure of default probabilities.

 $<sup>^{45}</sup>$ Note that this Distance to Default, which is the one commonly used in the literature, is measured in "log" units. In equation (2) we defined a related measure in levels to make it directly comparable to DI.

## D Realized versus Implied Volatility

As a robustness check on our empirical implementation of our DI measure, we compare median DI computed using realized and option-implied volatilities from option metrics. We focus on the median log DI since, as argued in Section 4.1, its fluctuations account for most of the fluctuations in the overall DI distribution. Figure 18 plots the time series of the median log DI measured using implied and realized volatility from OptionMetrics for the available data from 1996 to 2013. We use their daily data for both series to ensure that the same firms are included in both samples. We use the implied volatility from OptionMetrics' standardized, at the money, options with 30 days to maturity, and pool both calls and puts. The figure shows that realized volatility closely tracks fluctuations of implied volatility.

### **E** Firms with and without long-term debt

In this appendix we consider the evolution over the 1972-2012 time period of median measured DI for firms that have no long-term debt versus firms that do have long-term debt. We use data from Compustat to divide firms into these two categories.<sup>46</sup> Many of those firms that have no long term financial debt are in the pharmaceutical or computer industries.

In Figure S8, we show the median of DI (on a log scale) for those firms with no long term debt (in blue) and those firms with long term debt (in red). As is apparent in the figure, the collapse of median measured DI in the recent financial crisis was quite similar for these two groups of firms. Clearly, the level of firms' financial debt was not critical in determining the extent to which their measured DI declined in this time period. We also see that firms with no debt had substantially lower DI in the period surrounding the boom and bust of the tech industry in the late 1990's and early 2000's as would be expected given the concentration of firms with no long term debt in the computer industry.

<sup>&</sup>lt;sup>46</sup>Our data here are quarterly. The number of firms in CRSP/Compustat with no long term debt starts at roughly 150 in 1972, rises to nearly 1400 in the late 1990's and falls to between 800 and 900 over the past decade. In contrast, the number of firms with long-term debt is roughly 1700 in 1972, rises to nearly 5700 in the late 1990's, and falls to roughly 2700 at the end of the sample.



Figure S2: The empirical relationship between credit rating and measured DI.



Figure S3: The empirical relationship between measured DI and credit rating.



**Figure S4:** A scatter plot of monthly median measured DI versus monthly median Black and Scholes' Distance to Default by month and ratings class from December 1985 to December 2012. Each point represents a single month and data for one of seven ratings from AAA to CCC and below.



Figure S5: The distribution of measured DI, 1926–2012.



Figure S6: The 95th percentile of log measured DI 1926-2012 with time varying (red) versus constant (pink) standard deviation. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.



Figure S7: Asset volatility under the assumption of unlimited liability, and using Black and Scholes to compute the value of equity's default option, 1971-2012. In the calculation, we take  $V_B$  be equal to total liabilities, as in the unlimited liability calculations. The horizontal lines indicate the position of our benchmark cutoffs (DI=1,2,3,4) on the log scale.



Figure S8: The median of log DI for those firms with no long term debt (in blue) and those firms long term debt (in red), 1972-2012.

Name		Sample
American Express	Amex	01/02/1969 to today
American Insurance Group (AIG)	AIG	12/14/1972 to today
Bank of America	BOA	01/02/1969 to today
Bank of New York	BONY	12/04/1969 to today
Branch Banking and Trust	BB&T	12/14/1972 to today
Bear Stearns	BST	10/29/1985 to $05/30/2008$
Capital One	COF	11/16/1994 to today
City	$\mathbf{C}$	12/31/1925 to today
Fifth Third Bancorp	FITB	04/23/1975 to today
Fannie Mae	FNMA	08/31/1970 to $07/07/2010$
Freddy Mac	FRE	08/10/1989 to $07/07/2010$
Goldman Sachs	$\operatorname{GS}$	05/04/1999 to today
JP Morgan	JPM	03/05/1969 to today
Key Banks	KEY	02/23/1972 to today
Lehman Brothers	LEH	05/31/1994 to $09/17/2008$
Merrill Lynch	MERRILL	07/27/1971 to $12/31/2008$
MetLife	MET	04/05/2000 to today
Morgan Stanley	MS	03/21/1986 to today
PNC Financial Services	PNC	12/14/1972 to today
Regions Financial Corp	REG FIN	12/14/1972 to today
Suntrust Banks	SUNTRUST	07/01/1985 to today
State Street Boston Corporation	STATESTREET	12/14/1972 to today
US Bancorps	USB	12/14/1972 to today
Wachovia Corporation	WACH	12/14/1972 to $12/31/2008$
Washington Mutual	WaMu	03/11/1983 to $09/26/2008$

 Table 1: Government Backed Large Financial Institutions