Debt Constraints and Employment

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8th Banco de Portugal Conference on Monetary Economics

Motivation: US Great Contraction

- Characterized by drop in employment found to be
 - exceptionally large given observed drop in productivity **TFP**

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• highly persistent over time

Motivation: US Great Contraction

- Characterized by drop in employment found to be
 - exceptionally large given observed drop in productivity **TFP**
 - highly persistent over time

• This paper proposes a new mechanism that can produce such drop

• Within open economy model w/ consumer debt constraints

Our Mechanism

- Based on interplay between labor and consumer credit markets
- Key idea: workers become more productive with employment
 o working in current job raises productivity in all future jobs
- On-the-job HK acquisition implies returns to matching *backloaded* • substantial portion of match surplus materializes over time
- Backloading yields value of match surplus sensitive
 to changes in workers-firms discounting of income/profits
- So tightening of household debt constraints
 - by increasing discounting reduces value of match surplus

Why Are Returns to Matching Backloaded?

- $\bullet \ \ Time \ profile \ of \ returns \ central \ to \ our \ mechanism$
- This backloading naturally arises in our framework
- For a worker: a job provides
 - current wages
 - increment to future wages through human capital formation

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- For a firm: posting a vacancy entails
 - a cost today
 - stream of profits later once vacancy is filled

Main Results

- Tightening of debt constraints generates
 - large and persistent drop in employment
 - small drop in wages

- This stickiness of equilibrium wages arises *endogenously*
 - despite wages being continuously renegotiated
 - absence of any decline in aggregate productivity

• Consistent with aggregate/state-level evidence on US

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US Great Contraction

• Not only employment largely fell

• But also household debt to income ratio sharply contracted

- $\bullet~{\rm Regions~w/\,larger\,employment\,drop\,also\,larger\,fall\,in\,debt\,to\,income}$
 - Midrigan and Philippon (2011), Mian and Sufi (2014)

• Combined patterns: comovement consumption vs. employment

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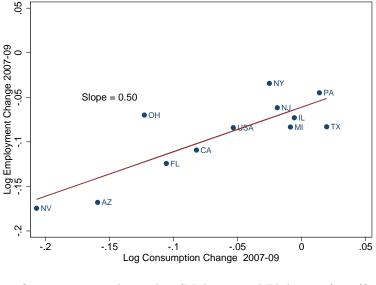
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Next: show comovement

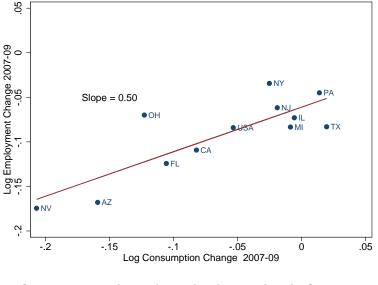
Employment vs. Consumption



Significant positive relationship (Midrigan and Philippon (2011)) $\Box \to \Box \to \Box \to \Box$

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Employment vs. Consumption



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Significant positive relationship: what has produced it?

US Great Contraction: Facts and Analysis

• Mian and Sufi (2014) document three facts

- 1. debt constraint tightening associated with house price fall
- 2. house price fall associated with regional employment drops
- $3. \ \ drops \, much \, more \, pronounced \, in \, nontradables \, than \, tradables$

- This paper first to propose general equilibrium model of US economy
 - tightening of household debt resulting from house price fall
 - $\circ~$ gives rise to large and persistent decline in employment
 - matches observed cross-sectional correlations (c_t, e_t, hp_t, d_t)
 - matches sectoral reallocation Mian and Sufi document

Overview

- Model US as open economy
- With DMP labor market characterized by
 - risk-averse consumers who can borrow and save
 - on-the-job human capital acquisition ("learning-by-doing")
 - household debt constraints
- Study one-time unanticipated tightening of debt constraints
 - one good economy: economy-wide shock (US recession)
 - $\circ~$ traded and non-traded goods economy: state-specific shocks
- Show model reproduces main aggregate-state patterns of recession

Related: Financial Frictions in Open Economies

- Traditional sudden stop model (Mendoza)
 - $\circ~$ credit friction on firm side
 - $\circ~$ amplify productivity shocks

Sticky wages (Guerrieri–Lorenzoni, Midrigan–Philippon)
 o credit friction on consumer side

- Sticky wages (Beraja, Hurst and Ospina)
 - $\circ~$ wages more sticky in time series than in cross section

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One-Good Economy

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Two Alternative Versions

- Financial frictions from either
 - debt constraints (no housing)
 - collateral constraints on housing
- Show two versions are equivalent
- Do so to emphasize
 - source of shock not important
 - $\circ~$ implied path for intertemporal MRS in consumption is

• Focus on collateral constraint interpretation

Economy

• Continuum of identical families

- Each family consists of continuum of workers
 - owns firms in the economy
 - pools idiosyncratic risk of workers
 - faces debt constraints

- Each worker in family
 - $\circ~$ characterized by idiosyncratic shock history s^t w.p. $\pi(s^t)$

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- earns $y(s^t)$ from market or home production
- $\circ~$ survives with probability ϕ

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Next: family maximization problem

Two-Part Family Problem

- Part I: choice of family-wide common consumption
 subject to debt constraints (version 1)
 - subject to collateral constraints on housing (version 2)

- Part II: choice by workers and family-owned firms
 of employment or no employment
 - $\circ~$ of vacancy creation

Part I: Problem with Debt Constraints

$$\max_{c_t} \sum_{t=0} \beta^t u(c_t)$$

$$c_t + qa_{t+1} = a_t + \int y_{it} di + D_t$$

$$a_{t+1} \ge -\overline{d}_t$$

- q: world price of one-period bond s.t. $\beta < q$
- y_{it} : income of worker *i* from wages or home production

- D_t : profits net of vacancy posting costs
- \overline{d}_t : debt limit

Part I: Problem with Collateral Constraints

$$\max_{c_{t},h_{t}} \sum_{t=0} \beta^{t} [u(c_{t}) + \psi_{t} v(h_{t})]$$

$$c_{t} + qa_{t+1} + p_{t}h_{t+1} = a_{t} + p_{t}h_{t} + \int y_{it} di + D_{t}$$

$$a_{t+1} \ge -\chi_{t} p_{t}h_{t+1}$$

- h_t : housing with price p_t in fixed supply H = 1
- q: world price of one-period bond s.t. $\beta < q$
- y_{it} : income of worker *i* from wages or home production

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- D_t : profits net of vacancy posting costs
- χ_t : maximum loan-to-value ratio

Equivalence Between Economies

- The two versions are equivalent
 - given $\{\overline{d}_t\}, \exists \{\psi_t\}$ s.t. allocations coincide
 - given $\{\psi_t\}, \exists \{\overline{d}_t\}$ s.t. allocations coincide
- Intuition
 - both generate same path for consumption
 - so generate same path for intertemporal MRS
 - intertemporal MRS all that matters for search part

• From now on: economy with collateral constraints

Part I: Problem with Collateral Constraints

$$\max_{c_{t},h_{t}} \sum_{t=0} \beta^{t} [u(c_{t}) + \psi_{t} v(h_{t})]$$

$$c_{t} + qa_{t+1} + p_{t}h_{t+1} = a_{t} + p_{t}h_{t} + \int y_{it} di + D_{t}$$

$$a_{t+1} \ge -\chi_{t} p_{t}h_{t+1}$$

- $Q_{t,t+1} = \beta^t u'(c_{t+1})/u'(c_t)$: family discount factor
- When a credit shock $(\psi_t \text{ or } \chi_t)$ hits and $c_t \downarrow : Q_{t,t+1} \downarrow$
- So workers and firms become endogenously more impatient
- $Q_{t,t+1}$ response crucial in propagating credit shock to economy

Part II: Worker and Firm Problem

- Workers: choose employment to maximize PV of income
 - using family's discount factor $Q_{t,t+1}$

$$\max\sum_{t=0}\sum_{s^t}\phi^t Q_{t,t+1}\pi(s^t)y(s^t)$$

• given idiosyncratic shock history $s^t = (s_0, s_1, \dots, s_t)$

- s_t : records idiosyncratic events at t (affecting lifetime)
 - birth/death
 - separation/matching
 - human capital shock
- Firms: choose vacancies to maximize PV of profits
 also discounted using family's discount factor Q_{t,t+1}

Human Capital and Output Technologies

• Newborns enter with human capital

$$\log(z) \sim N(0, \sigma_z^2/(1-\rho_z^2))$$

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$$\log(z) \sim N(0, \sigma_z^2/(1-\rho_z^2))$$

• On-the-job human capital accumulation/off-the-job depreciation • employed worker's z evolves according to $F_e(z'|z)$: drifts up

$$\log z' = (1 - \rho_z)\mu_z + \rho_z \log z + \sigma_z \varepsilon'$$

• non-employed worker's z according to $F_u(z'|z)$: drifts down

$$\log z' = \rho_z \log z + \sigma_z \varepsilon'$$

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$$\log z' = \rho_z \log z + \sigma_z \varepsilon'$$

- Employed consumers: produce z and receive wage $w_t(z)$
- Non-employed consumers: produce b (same w/ output prop'l to z)

Matching Technology

- Matching function: $M(u_t, v_t) = Bu_t^{\eta} v_t^{1-\eta}$
- Market tightness: $\theta_t = v_t/u_t$
- Probability firm finds worker

$$\lambda_{f,t} = \frac{M(u_t, v_t)}{v_t} = B\left(\frac{u_t}{v_t}\right)^{\eta} = B\theta_t^{-\eta}$$

• Probability worker finds firm

$$\lambda_{w,t} = \frac{M(u_t, v_t)}{u_t} = B\left(\frac{v_t}{u_t}\right)^{1-\eta} = B\theta_t^{1-\eta}$$

• Probability match exogenously destroyed: σ

Worker Values

• Employed consumer's value: $W_t(z)$ equals

$$w_{t}(z) + \phi Q_{t,t+1} (1 - \sigma) \int_{z'} \max \left[W_{t+1}(z'), U_{t+1}(z') \right] dF_{e}(z'|z) + \phi Q_{t,t+1} \sigma \int_{z'} U_{t+1}(z') dF_{e}(z'|z)$$

• Unemployed consumer's value: $U_t(z)$ equals

$$b + \phi Q_{t,t+1} \lambda_{w,t} \int_{z'} \max \left[W_{t+1} \left(z' \right), U_{t+1} \left(z' \right) \right] dF_u \left(z' | z \right) + \phi Q_{t,t+1} \left(1 - \lambda_{w,t} \right) \int_{z'} U_{t+1} \left(z' \right) dF_u \left(z' | z \right)$$

• Consumer discount factor \downarrow when debt constraint binds

Firm Value

• Value of a vacancy filled with worker with human capital z

$$J_{t}(z) = z - w_{t}(z) + \phi Q_{t,t+1}(1 - \sigma) \int_{z'} \max \left[J_{t+1}(z'), 0 \right] dF_{e}(z'|z)$$

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• Firm discount factor \downarrow when family debt constraint binds

Equilibrium Wages

- Wages renegotiated period by period
- Determined by generalized Nash bargaining

$$\max_{w_t(z)} \left[W_t(z) - U_t(z) \right]^{\gamma} J_t(z)^{1-\gamma}$$

s.t.

$$\frac{\gamma}{W_t(z) - U_t(z)} = \frac{1 - \gamma}{J_t(z)}$$

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- γ : worker's bargaining weight
- Similar results with alternating offer bargaining

Free-Entry Condition

• Firms pay κ units of output to post a vacancy

• Due to firm competition, expected value of filling vacancy equals κ

• Let
$$n_t^u(z)$$
 measure of unemployed so $\tilde{n}_t^u(z) = \frac{n_t^u(z)}{\int dn_t^u(z)}$
 $\kappa = \phi Q_{t,t+1} \lambda_{f,t} \int_{z'} \max \left[J_{t+1}(z'), 0 \right] dF_u(z'|z) d\tilde{n}_t^u(z)$

- Pins down vacancy to unemployment ratio θ_t
- Provides intuition for how debt tightening affects vacancy creation

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Impact of Credit Shock on Vacancy Creation

- When debt constraint binds: $u'(c_t) \uparrow$ implies $Q_{t,t+1} \downarrow$
- Decrease in $Q_{t,t+1}$ depresses firms' incentives to post vacancies
- Since it leads to fall in expected profits from filling vacancy

$$\kappa = \phi Q_{t,t+1} \lambda_{f,t} \int_{z'} \max \left[J_{t+1} \left(z' \right), 0 \right] dF_u \left(z' | z \right) d\tilde{n}_t^u \left(z \right)$$

• Or, equivalently, to rise in cost of posting vacancies (in utils)

$$\kappa u'(c_t) = \beta \phi u'(c_{t+1}) \lambda_{f,t} \int_{z'} \max \left[J_{t+1}(z'), 0 \right] dF_u(z'|z) d\tilde{n}_t^u(z)$$

Impact of Credit Shock on Workers

- $\bullet~$ Quantitatively: worker side effect much more important than firm
- Workers' value
 - current wages: more
 - increment to human capital: less
- In Nash bargaining
 - workers want higher current wages
 - firms want lower current wages
 - in equilibrium wages endogenously sticky

so vacancies contract

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Next: model parameterization via external and internal calibration a sage

Assigned Parameters

- Period 1 quarter ($\beta = 0.94^{1/4}$ and $q = 0.96^{1/4}$)
- Survival rate so consumers in market for 40 years
- Probability of separation: $\sigma = 0.10$ as Shimer (2005)
- Bargaining share and matching elasticity: $\gamma = \eta = 0.5$

•
$$u(c_t) = c_t^{1-\alpha}/(1-\alpha)$$
 with $\alpha = 5$ so IES = 0.2

- Attanasio et al. (2002): 0.1 < IES < 0.2 (non-stockholders)
- Vissing and Jorgensen (2002): IES ≈ 0 (non-stockholders)
- Hall (1988): IES < 0.1

Jointly Calibrated Parameters more

- Efficiency matching function: B
 - \rightarrow employment-population ratio = 0.8 (U.S. age 25-54)
- Home production: *b*

 $\rightarrow b/\text{median } w = 0.4 \text{ (Shimer (2005))}$

• Std. dev. of shocks to z: σ_z

 \rightarrow std. dev. of log wage changes = 0.21 (Floden et al. (2001))

• Persistence shocks to z: ρ_z

 \rightarrow std. dev. of log initial wages = 0.94 (PSID)

• Returns to employment: μ_z

 \rightarrow returns to tenure-experience (Buchinsky et al. (2010))

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Returns to Tenure and Experience

- Indirect inference approach to quantify these returns
- That allows for varying degrees of portability of acquired skills
- Using empirical wage model of BFKT (2010) as auxiliary model
- Compute for each model-simulated path, wage predicted by BFKT $\widehat{\log(w_{it})} = \widehat{f}(\text{experience}_{it}) + \widehat{g}(\text{tenure}_{it}) + \widehat{\Psi}_{it}(\cdot)$
- Ψ_{it} summarizes employment history at previous jobs l

$$\Psi_{it} = \sum_{l=1}^{M_{it}} \sum_{k=1}^{4} \left(\phi_k^0 + \phi_k^s \text{tenure}_i^l + \phi_k^e \text{experience}_i^l \right) d_{ki}^l$$

• Captures different degrees of transferability of HK across matches

Returns to Tenure and Experience

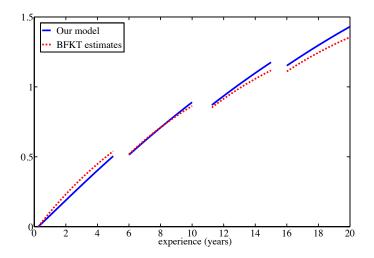
- Minimize distance between
 - $\Delta \log(w_{it})$ predicted by BFKT for simulated experience/tenure

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• $\Delta \log(w_{it})$ implied by our simulated model

• Resulting wage growth: 5.2% per year

Returns: Model vs. BFKT Estimates



Initialize w/ zero exp., mean z_{it} at zero exp. and no shocks

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Experiment: Economy-Wide Credit Crunch

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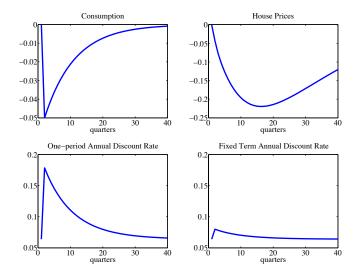
Experiment: Economy-Wide Credit Crunch

- Assume unanticipated drop in taste for houses ψ_t (alternative)
- With binding debt constraint: $a_{t+1} = -\chi p_t h_{t+1}$
- Choose path for ψ_t so c_t falls 5% then mean reverts as

$$\Delta c_t = \rho \Delta c_{t-1}$$

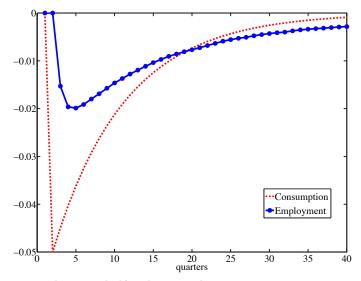
- $\rho = 0.90$ calibrated to match speed of postwar recoveries
- Show impact on consumption, house prices, and employment

Experiment: Economy-Wide Credit Crunch



BR panel: change in constant rate giving rise to the same PV

Employment vs. Consumption



Drop in employment half as large as drop in consumption at impact 200

Employment Response

• Employment drop much more persistent

• Use cumulative impulse responses (CIR)

~ 2 years. Cite = 11/0 of Cite	0	2 years:	$CIR_E =$	44%	of	CIR
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- \circ 10 years: CIR_E = 69% of CIR_C
- \circ overall: CIR_E = 92% of CIR_C
- Employment decline of magnitude comparable to c_t drop
- Employment drop mostly accounted for \downarrow in vacancy creation

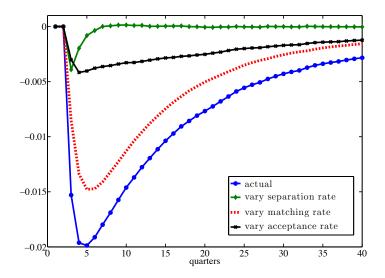
Decomposition of Employment Response

• Shimer (2012) approach

$$E_{t+1} = (1 - s_t)E_t + \lambda_{w,t}x_t(1 - E_t)$$

- \circ s_t: separation rate
- $\lambda_{w,t}$: worker matching rate
- x_t : acceptance rate
- Construct three counterfactual employment series
 - vary s_t , $\lambda_{w,t}$, x_t in isolation
 - leave others at steady state values
- Drop in $\lambda_{w,t}$ most accounts for drop E_t

Decomposition of Employment Response



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Why Is Employment Drop Persistent?

Selection effect

- as worst matches endogenously dissolved
- average productivity of unemployed decreases
- this effect further lowers returns to posting a vacancy

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• Credit shock persistent

• Each accounts for about 1/2 of persistence in drop

Key Forces Behind Employment Drop

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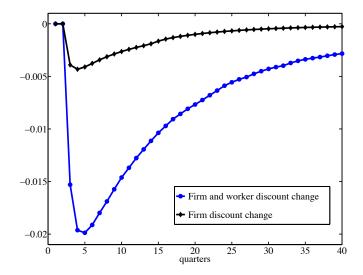
• Endogenous wage stickiness

• Returns to tenure and experience

Key Force I: Endogenous Wage Stickiness

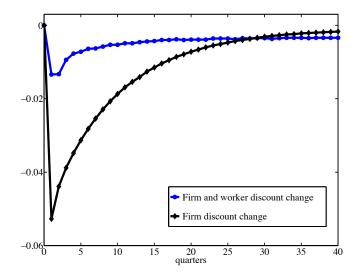
- Wages \approx constant when firms-workers' discount factors decrease
- Unlike most search models that feature 'Shimer' puzzle
 - negative shock leads to large drops in wages
 - $\circ~$ no drop in employment
- Our model does *not* feature 'Shimer puzzle'
 - reason: fall in discounting disproportionally hurts workers
 - $\circ~$ HK transferable: fall affects their returns over longer horizon
 - $\circ~$ as it depresses expected value of wages from $\,all$ future matches
 - so for workers to agree to match, wages cannot fall
- Indeed if only workers' discount factors decreased: wages \uparrow

Employment: Firm and Worker Discounting



Employment falls much more when consumer discount factor changes $\exists a \to a = b = a = b$

Wages: Firm and Worker Discounting



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Since wages do not fall much

Key Force II: Returns to Tenure and Experience

• Makes returns from matching backloaded

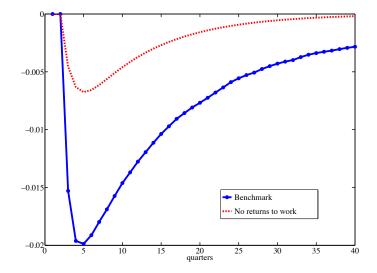
• Backloading critical to amplifying effect of credit shocks

• Negligible employment effects w/o returns to employment

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• Illustrate by making worker output, z, constant

Employment Profile with Varying Returns



Without returns drop would be 1/4 of the drop with such returns

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Explains Small Effect of Hall (2014)

• Risk-neutral firms and workers

• Workers produce constant output

• Fixed-term discount rate 10% to 20%: $u_t \, {\rm from} \, 5.8\% \, {\rm to} \, 5.88\%$

• So no effect on u_t despite shock *four times* as large as ours

• In our model fixed-term discount rate \uparrow from 6% to 8.5%

Economy with Traded and Non-traded Goods

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Consumer Credit Crunch Conjecture

- Commonly thought contraction in consumer credit key to recession
- Mian and Sufi document recession at state level characterized by
 - fall in house prices
 - decline in *nontraded* employment highly correlated with it
 - $\circ~$ drop in traded employment largely unrelated to it
- Conjecture patterns consistent w/tightening of consumer borrowing

- Argue *exogenous rigidities* may be needed to account for them
- Can our model account for these patterns?

Economy with Traded and Non-traded Goods

- Suppose each US state produces
 - $\circ~$ common traded good
 - state-specific non-traded good

• Labor cannot move across states but can switch sectors

Study response to state-specific shocks to debt constraints
 to evaluate model against Mian and Sufi (2014) evidence

Preferences

• Preferences in a state

$$\sum_{t=0}^{\infty} \beta^t [u(c_t) + \psi_t v(h_t)]$$

• c_t : aggregate of state non-traded (N) and of traded (T)

$$c_{t} = \left[\tau^{\frac{1}{\sigma}} \left(c_{Nt}\right)^{\frac{\mu-1}{\mu}} + (1-\tau)^{\frac{1}{\sigma}} \left(c_{Tt}\right)^{\frac{\mu-1}{\mu}}\right]^{\frac{\mu}{\mu-1}}$$

• Traded goods imported from rest of the world at price of 1

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• Firms owned internationally (no firm discount effect)

Output and Search Technologies

• Two sectors: traded (T) and non-traded (N) goods

• Produce z units of traded or non-traded goods

• Matching according to sector-specific technologies

$$M_{Tt} = B_T(u_t)^{\eta} (v_{Tt})^{1-\eta}$$
 and $M_{Nt} = B_N(u_t)^{\eta} (v_{Nt})^{1-\eta}$

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• Simultaneous search in both sectors (at most one offer)

Tightening Debt Constraints in a State

• Decreases demand for state non-traded goods

• price of non-traded falls relative to price of traded goods

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- No effect on demand for state traded goods
 - $\circ~$ employment in non-traded drops a~lot
 - employment in traded drops a *little*
 - $\circ~$ as observed in the data

Tightening Debt Constraints in a State

• Decreases demand for state non-traded goods

• price of non-traded falls relative to price of traded goods

- No effect on demand for state traded goods
 - $\circ\,$ employment in non-traded drops $a\ lot$
 - employment in traded drops a *little*
 - $\circ~$ as observed in the data
- So model qualitatively matches patterns of Mian and Sufi

Tightening Debt Constraints in a State

• Decreases demand for state non-traded goods

- $\circ~$ price of non-traded falls relative to price of traded goods
- No effect on demand for state traded goods
 - $\circ~$ employment in non-traded drops a~lot
 - employment in traded drops a *little*
 - $\circ~$ as observed in the data
- Will show model also quantitatively replicates observed changes in
 - nontradable employment across states
 - $\circ~$ tradable employment across states

in response to credit tightening (next: quantify these effects)

Additional Parameters

- Calibrate so same steady state predictions as in one-sector
- Preferences weight on non-traded goods so that
 2/3 employment in non-traded as in Mian and Sufi (2014)

- Elasticity traded vs. non-traded goods: $\mu = 4$
- Choose B_T , B_N , κ_T and κ_N so that
 - $\circ~$ employment to population ratio: 80%
 - steady state $p_T = p_N$ and $\omega_T(z) = \omega_N(z)$

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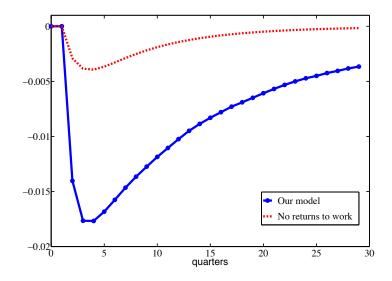
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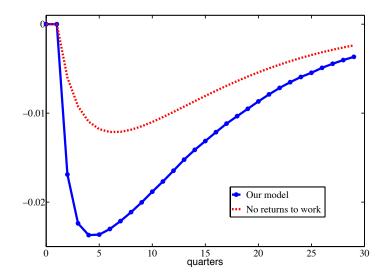
Next: examine effect of fall in housing taste in a state so $c_t \downarrow by 5\%$

Employment



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Nontradable Employment



Experiment Motivated by Mian and Sufi (2014)

- To assess model ability to account for differential response of
 - $\circ~$ nontradable and tradable employment $across~{\rm states}$

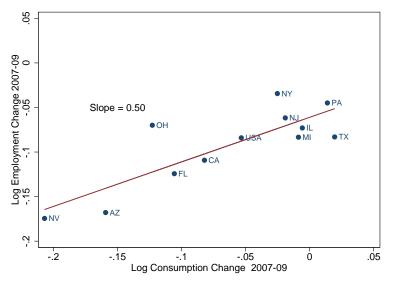
- Assume differential fall in housing taste in 20 states so that
 - $\circ~$ State 1: consumption falls 1%

. . .

 $\circ~$ State 20: consumption falls 20%

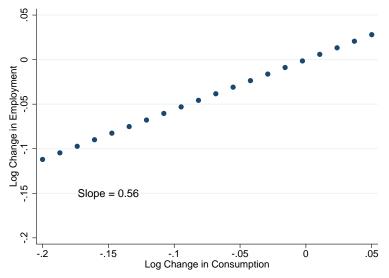
Next: predicted change in employment and consumption? = , = $\circ \circ \circ$

Employment vs. Consumption: Data



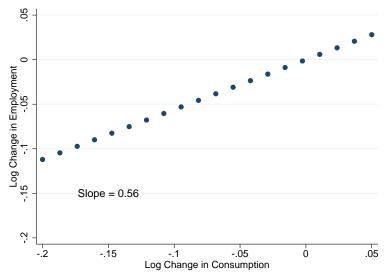
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Employment vs. Consumption: Model



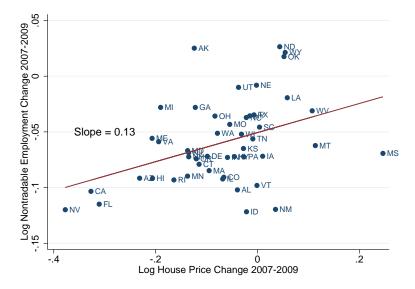
Model captures this comovement fairly well (similar elasticity)

Employment vs. Consumption: Model



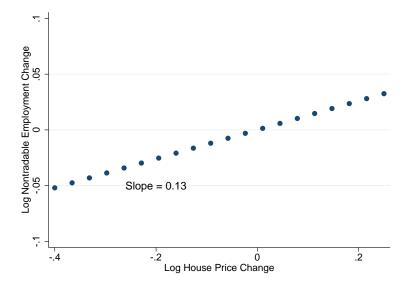
Next: how does employment respond to changes in house prices?

Nontradable Emp. vs. House Prices: Data



Nontradable emp't fell more in states with greater house price fall

Nontradable Emp. vs. House Prices: Model



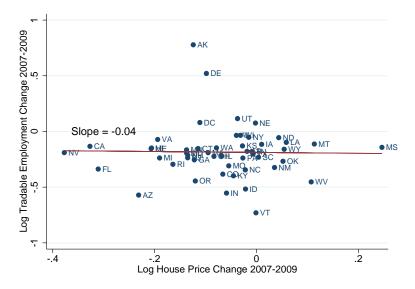
Model reproduces the slope of predicted linear relationship

Nontradable Emp. vs. House Prices: No Returns

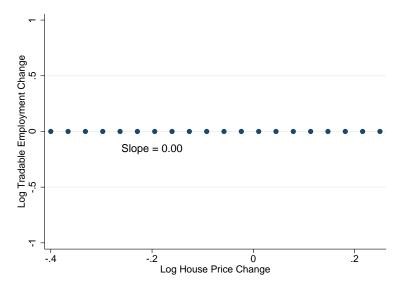


Model would produce smaller sensitivity (0.07 vs. 0.13 in data)

Tradable Employment vs. House Prices: Data

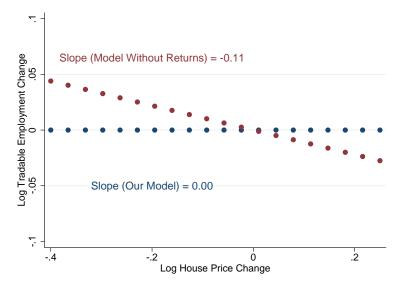


Tradable Employment vs. House Prices: Model



Model matches well the uniform response of tradable employment

Tradable Emp. vs. House Prices: No Returns



Would be at odds with tradable emp't response $(-0.11 \text{ vs. } 0 \text{ in data})_{=}$

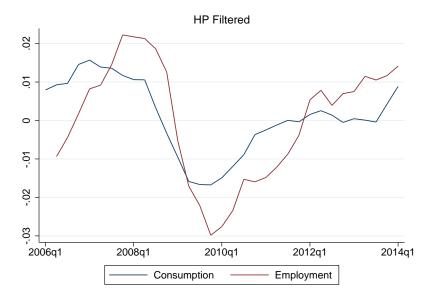
Conclusion

- Key idea
 - when returns to employment are backloaded
 - employment sensitive to changes in debt constraints

- Showed in DMP model this force
 - generates endogenously sticky wages
 - amplifies employment drop due to tighter debt constraints

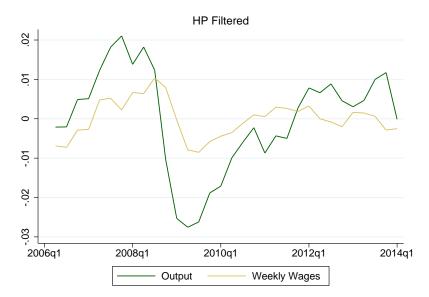
- Quantitatively promising mechanism to account for
 - aggregate US evidence
 - cross-regional US evidence

US Great Contraction



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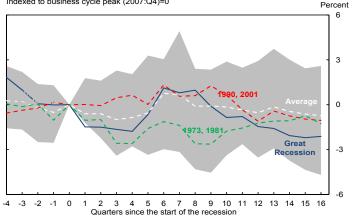
US Great Contraction



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US Great Contraction

F. Utilization-Adjusted TFP Indexed to business cycle peak (2007:Q4)=0



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Further Model Implications

Fraction workers with $w < b$	0.180
Prob. job destroyed endogenously	0.002
Prob. worker matches (λ_w)	0.595
Fraction matches with positive surplus	0.722
Drop in w if unemployed 1 year	0.063

Other implications broadly in accord with the data (back)

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Experiment: Economy-Wide Credit Crunch

• Our experiment

 $\circ~$ reduce taste for houses ψ_t

 $\circ~$ keep LTV parameter χ constant

• Alternative

- $\circ~$ keep taste for houses ψ_t constant
- $\circ~$ reduce LTV parameter χ

• Nearly identical results

Generate Consumption Path From LTV Ratios

• Use budget constraint, $h_t = 1$, binding debt constraint

$$c_t = y_t + \chi p_t - \chi p_{t+1}$$

• And Euler equation

$$\beta \phi \psi v'(1) = p_t u'(c_t) - \beta \phi p_{t+1} u'(c_{t+1}) - \chi p_t \mu_t$$

• With multiplier on debt constraint

$$\mu_t = u'(c_t) - \beta \phi q u'(c_{t+1})$$

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• So χ path generates desired c_t path back

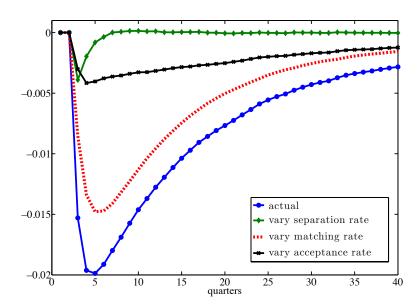
Employment Decomposition

• Shimer (2012) approach

$$E_{t+1} = (1 - s_t)E_t + \lambda_{w,t}x_t(1 - E_t)$$

- \circ s_t: separation rate
- $\lambda_{w,t}$: worker matching probability
- \circ x_t : acceptance rate
- Construct three counterfactual employment series
 - vary s_t , $\lambda_{w,t}$, x_t in isolation
 - leave others at steady state values

• Drop in $\lambda_{w,t}$ accounts most of drop E_t



Results Not Driven by Lower Acceptance

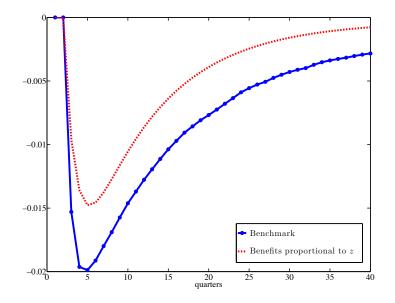
- Illustrate by making home production proportional to \boldsymbol{z}_t
 - $\circ \ b_t = \lambda z_t$
 - $\circ~$ choose λ s.t. home production is 40% of shadow wage

• Unemployed accept all jobs and no endogenous separation

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• Employment drop is 3/4 of drop in benchmark

Results Not Driven by Lower Acceptance **back**



Why Is Employment Drop Persistent?

• Selection effect

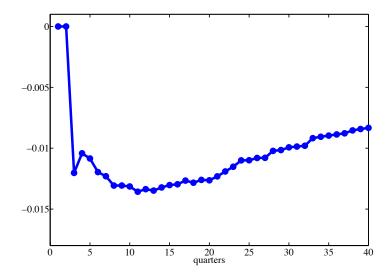
- worst matches endogenously dissolved
- lower average productivity of unemployed
- lower returns to posting a vacancy

• Credit shock persistent

• Each accounts for about 1/2 of persistence in drop

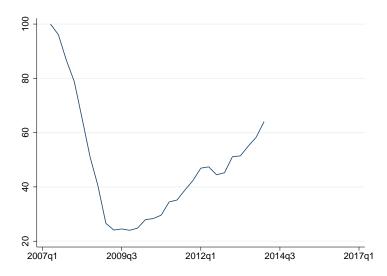
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Average Productivity of Unemployed



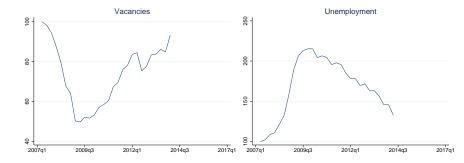
Productivity of unemployed falls as worse matches are dissolved back

Market Tightness: Data



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Vacancies and Unemployment: Data (back)



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