# Efficient Perceptual Coding and Reference-Dependent Valuations

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### **Reference-Dependent Valuations**

• Experimentally observed choices not always consistent with the existence of consistent preferences over final outcomes (independent of path by which they are reached)

— a key feature of the prospect theory of Kahneman and Tversky (1979)

# Kahneman-Tversky (1979)

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In addition to whatever you own, you have been given 1000. You are now asked to choose between (a) winning an additional 500 with certainty, or (b) a gamble with a 50 percent chance of winning 1000 and a 50 percent chance of winning nothing.

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In addition to whatever you own, you have been given 2000. You are now asked to choose between (a) losing 500 with certainty, and (b) a gamble with a 50 percent chance of losing 1000 and a 50 percent chance of losing nothing.

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Majority of subjects choose (a)

#### Problem

In addition to whatever you own, you have been given 2000. You are now asked to choose between (a) losing 500 with certainty, and (b) a gamble with a 50 percent chance of losing 1000 and a 50 percent chance of losing nothing.

#### Majority of subjects choose (b)

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## Kahneman-Tversky (1979)

 Problem for standard EU theory: in both cases, subjects are choosing between the same probability distributions over final wealth levels:

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 Explanation proposed by prospect theory: people don't evaluate only distribution over final situations, they care about distribution of gains or losses relative to "reference point" (wealth prior to the choice)

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- Alternative proposal here: standard preferences, but choice based on imperfect perception of available options
- Idea: reference-dependence a feature of the way objective characteristics are mapped into subjective representations
  - this can be optimal, due to constraints on information-processing capacity

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  - similar patterns observed in many different sensory domains

— suggesting common processing constraints may be responsible for usefulness of similar computational strategies in multiple contexts

#### Imperfect Sensory Perception

- Long experimental literature in psychophysics shows that discrimination between stimuli is both imprecise and probabilistic:
  - probability of correct discrimination of relative brightness, direction of motion, etc., increasing function of objective difference ("psychometric function")

## Motion Discrimination: Britten et al. (1992)



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- Interpretation: relation between objective characteristics of stimulus and subjective representation is stochastic
  - in animals, the stochastic relationship between stimulus and neural coding can be directly observed
  - e.g., Britten *et al.* (1992) study of ability of rhesus monkeys to discriminate the direction of motion of moving dots

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  - common experience: adjustment of vision to dark room, or bright sunlight
  - experiment: prolonged exposure to a particular stimulus leads to increased discriminability of stimuli similar to the adaptor, but reduced discriminability of stimuli farther from it

#### Post-Adaptation Discrimination Thresholds



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  - after-effects from prolonged exposure to an intense stimulus: brightness, color, tilt of lines, direction of motion, etc.

#### Repulsion Effect: Direction of Motion



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  - after-effects from prolonged exposure to an intense stimulus: brightness, color, tilt of lines, direction of motion, etc.
  - similar repulsion effects from other elements of visual field: many common visual illusions

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#### Perceived Brightness Depends on Contrast



#### The central squares reflect equal amounts of light.

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### Perceived Orientation Depends on Contrast



The central bars are actually vertical.

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## Explaining Sensory Adaptation

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- Proposal: perceptual coding adjusts to the (apparent) frequency distribution of stimuli in a given environment (class of situations)
- It does this so as to make efficient use of limited information-processing capacity of the channel over which observations of the world must be transmitted to the nervous system

#### Levels of Processing



#### Efficient Perception

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### **Efficient Perception**

- Concern here: how a subjective representation r of the situation is produced, as function of the actual state s, and the prior [distribution f(s)] for this class of situations
  - note: the mapping from s to r will be stochastic
- Hypothesis: the perceptual mapping is efficient, given
  - the decision problem [defined by U(s, a), a to be a function of r]
  - the prior f(s)
  - capacity of the channel for transmission of information about *s* used to produce *r*

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- Given these properties, the (Shannon) capacity of the channel is defined as

$$C(p) \equiv \max_{\pi} I_{\pi}(X, R)$$

where for any frequency distribution  $\pi(x)$  over inputs x,  $I_{\pi}$  is the mutual information between random variables X and Rwhen joint distribution is  $p(x, r) = \pi(x)p(r|x)$
- Complete perception/action circuit:
  - encoding: x = g(s)
  - transmission [perception]: r produced with prob p(r|x)
  - decoding [action]: a = h(r)

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  - encoding: x = g(s)
  - transmission [perception]: r produced with prob p(r|x)
  - decoding [action]: a = h(r)
- Relevant measure of accuracy of perception: given joint distribution for (s, r) implied by prior f, encoding g, and channel p,

$$W(g, p; f) \equiv \mathrm{E}_{s,r} \left[ \max_{h(r)} \mathrm{E}_{s'} [U(h(r), s') | r] \right]$$

Two (nested) efficiency hypotheses:

Efficient Coding Hypothesis: the encoding function g is optimized for the prior f and channel p

$$\hat{W}(p;f) \equiv \max_{g} W(g,p;f)$$

• implies adaptation of g (hence joint dist'n p(s, r)) to changing environment f

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Efficient Coding Hypothesis: the encoding function g is optimized for the prior f and channel p

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- implies adaptation of g (hence joint dist'n p(s, r)) to changing environment f
- Efficient Channel Hypothesis: the channel p is also optimized, for some prior over states, subject to a bound on possible channel capacity

$$\max_{p} \hat{W}(p; f) \quad \text{s.t.} \ C(p) \leq \bar{C}$$

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  - hence p may be optimal for typical past environment, but not current f
  - or p may be optimized for a class of possible environments  $\{f_{\theta}\}$ , given prior over parameters  $\theta$

$$\max_{p} \mathrm{E}_{\theta} \hat{W}(p; f_{\theta})$$

Illustrative application:

- State  $\theta$  = direction of motion of stimulus (angle on the circle)
- Action: estimated direction  $\hat{ heta}$  (also an angle on the circle)
- Objective: maximization of expected accuracy

$$\mathrm{E}[\cos(\hat{\theta} - \theta)]$$

• approximately minimization of MSE, when accuracy is high: but a periodic function

• Channel: assumed to be optimized for a uniform prior

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$$f(\theta) = 1/2\pi \quad \forall \theta$$

- Optimal channel:
  - input space = angles  $\hat{\phi}$  on the circle
  - optimal encoding [wlog]:  $\hat{\phi}(\theta) = \theta$
  - output space = angles  $\phi$  on the circle
  - distribution of outputs [subjective perceptions of direction] given input:

$$p(\phi|\hat{\phi}) = A e^{\lambda^{-1}\cos(\phi - \hat{\phi})} \quad \forall \phi$$

where  $\lambda > 0$  varies inversely with capacity  $\bar{C}$ 

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$$f(\theta) = B \ e^{\beta \cos \theta}$$

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• Numerical example:  $\lambda = 1, \beta = 0.8$ 

# Post-Adaptation Prior



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#### Post-Adaptation Optimal Coding



#### Post-Adaptation Optimal Decoding



Predictions for experimental data:

• Effect of adaptation on perceived direction of motion:

- define the average perceived direction  $\bar{\phi}$  (given distribution of representations  $\phi$ ) as the angle that max's  $E_{\phi}[\cos(\phi \bar{\phi})]$
- then measure bias by

$$\mathsf{bias}(\theta) \equiv \bar{\phi}(\theta) - \theta$$

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Iffect on sensitivity to differences in direction of motion:

• measure the variability of perceived direction by

$$\sigma_{\phi}^2 \equiv 2\{1 - \mathrm{E}[\cos(\phi - \bar{\phi})]\}$$

• then define the discrimination threshold function by

$$\tau(\theta) \equiv \frac{\sigma_{\phi}(\theta)}{\bar{\phi}'(\theta)}$$

# Prediction: Repulsion Effect



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#### Evidence: Repulsion Effect



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# Prediction: Sensitivity Effect



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#### Evidence: Sensitivity Effect



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• Model: suppose that true utility value of each option is a sum

$$u = \sum_{a} s_{a}$$

of the values of each of a number of attributes, each of which must be perceived separately

## Perceptions of Value

- Assumed form of channel:
  - a subjective perception  $r_a$  for each attribute
  - parallel processing: conditional probabilities  $p_a(r_a|x_a)$  for each attribute are independent of other attributes, where  $x_a$  is a function only of  $s_a$

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- Assumed objective: minimize MSE of subjective estimate of *u*
- Assume priors are independent for each attribute

$$f(\overrightarrow{s}) = \prod f_a(s_a)$$

### Optimal Perception of Value

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## **Optimal Perception of Value**

• Optimal decoding of each attribute depends only on prior, coding, and channel for that attribute:

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- Optimal coding of attribute a depends only on  $f_a$ ,  $p_a$
- Optimal channel for attribute *a* depends only on  $f_a$  and shadow value  $\lambda$  of additional capacity (same for all attributes)

 Suppose different possible classes θ of choice situations are associated with different priors f<sup>θ</sup> over possible values of the attributes; but suppose that prior for attribute a is of the same form

$$f_{a}^{\theta}(s_{a}) = rac{1}{\sigma_{a}} \hat{f}_{a} \left( rac{s_{a} - \mu_{a}^{ heta}}{\sigma_{a}^{ heta}} 
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for all  $\theta$ 

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• Then given channel  $p_a$ , optimal coding will be of same form

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- Hence coding of value will be reference-dependent: what is coded is not absolute value  $s_a$ , but  $s_a$  relative to the prior mean
  - the "reference point" is thus determined by expectations, as argued by Koszegi and Rabin (2006)
  - but in general, no significance of any single "reference point": coding is relative to the prior distribution

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- Generally only a finite number of output states
  - hence little difference in the way that extreme states (relative to the prior) are coded
  - how far into the tails of prior states continue to be distinguished depends on capacity allocated to perception of the attribute in question

#### Mean Subjective Value vs. True Value



# Kahneman-Tversky (1979) Example

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- (b) 50 percent chance of initial wealth + 1000, 50 percent chance of initial wealth + 2000
- Explanation proposed by "prospect theory": outcomes evaluated relative to a different reference point in the two cases (wealth prior to the choice)

• Choice between two lotteries: the relevant attributes of each are its payoffs in the two equi-probable states

(a) (1500, 1500) (b) (1000, 2000) • Choice between two lotteries: the relevant attributes of each are its payoffs in the two equi-probable states

(a) (1500, 1500) (b) (1000, 2000)

• Subjective perception of each of the two attributes depends on distribution of expected possible values for that attribute

# Applying the Theory

- Suppose the class  $\theta$  for which perceptual coding is optimized is "choice between two lotteries, starting from initial wealth  $\theta$ "
  - prior  $f^{\theta}$  is evoked by receipt of initial payment  $\theta$  (the "cue"), before presentation of lotteries

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  - distribution of possible lottery payoffs in each state is expected to be independent of initial wealth
- Efficiency hypothesis:
  - channel is optimized for the entire class of possible priors {f<sup>θ</sup>} (prior over θ doesn't matter!)
  - encoding optimally adapts to the particular prior  $f^{\theta}$  after initial wealth  $\theta$  is learned

#### Mean Subjective Valuations of Options



(a) has higher MNSV when  $\mu^{ heta}=$  1000, but (b) higher when  $\mu^{ heta}=$  2000

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Explanation by a sigmoid-shaped "value function" formally the same, though here the nonlinear transformation interpreted as reflecting perception rather then preferences. Also:

- Deeper explanation for shape of the value function proposed
- Provides a theory of location of "reference point"

— and not always status quo

 Predicts that both reference-dependence, and departures from risk-neutrality for small gambles, will be greater in contexts where stakes are small enough for low-capacity channel to be optimal

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  - in above case, would be optimal to code only mean outcome over states ⇒ (a) and (b) equivalent
- RI assumes upper bound on mutual information rather than channel capacity
  - in above case, optimal coding would make  $E[\hat{z}|z]$  a linear function  $\Rightarrow$  (a) and (b) have same MNSV

- The efficient coding hypothesis simultaneously offers candidate explanation for other behavioral anomalies:
  - stochasticity of choice

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"focusing effects"

- optimal channel may transmit no information at all about some utility-relevant attributes (corner solution)

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"focusing effects"

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• "menu effects"

— if prior implies correlation of attributes of choices in a given choice set

- A variety of modifications of standard choice theory have been proposed to allow for each of these anomalies:
  - random utility models (McFadden, 1974)
  - prospect theory (Kahneman-Tversky, 1979)
  - reference-dependent preferences (Koszegi-Rabin, 2006)
  - preference for sparse representations (Gabaix, 2010)
  - range-dependent weights on attributes (Koszegi-Szeidl, 2011)
  - "local thinking" (Bordalo et al., 2010, 2011)
  - preferences depend on "comparison set" (Cunningham, 2011)

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  - "local thinking" (Bordalo et al., 2010, 2011)
  - preferences depend on "comparison set" (Cunningham, 2011)
- But the present proposal offers a unified explanation of all of these phenomena

— in a way that is also consistent with observations about perception in other contexts

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