# A Model of Moral-Hazard Credit Cycles

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Model

$$\sum_{s=0}^{n-1} r_{t+s+1}(I_{t+s}) = \mathsf{pdv} \text{ of bribe} + \mathsf{opportunity cost} (\mathsf{per unit})$$

Model

$$\sum_{s=0}^{n-1} r_{t+s+1}(I_{t+s}) = X$$

Model

$$\sum_{s=0}^{n-1} r_{t+s+1}(I_{t+s}) = X$$

Not

$$\sum_{s=0}^{n-1} \gamma^{s} r_{t+s+1}(I_{t+s}) = X$$

Model

$$\sum_{s=0}^{n-1} r_{t+s+1}(I_{t+s}) = X$$

Comes from

$$\sum_{s=0}^{n-1} \left(\frac{\alpha}{1+\rho_I}\right)^s r_{t+s+1}h_s$$

$$h_s = \left(\frac{1+\rho_b}{\alpha}\right)^s$$

Model

$$\sum_{s=0}^{n-1} r_{t+s+1}(I_{t+s}) = X$$

Requires:

- Investors and bankers have same discount factor
- All bribe payments come at the end of bankers' careers.

Can the model be closed without losing the multiplicity of equilibria?

• Does smoothing elsewhere (labor market, optimal intertemporal consumption, investment) eliminate the cyclical paths?

#### **Question 2: What causes cycles?**

Statement: When trusted bankers become scarce aggregate investment must decline.

- But bankers in elastic supply in this model
- Rather recessions caused by expectations of booms

$$\sum_{s=0}^{n-1} r_{t+s+1}(I_{t+s}) = X$$

• What the cohort structure gives you is a reason to expect a future boom.

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- This makes the model very flexible.
- How do we test it?

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Possibilities:

- Relationship between cohort structure of financial sector and investment.
- Relationship between bribe and variance of gross returns.
  - ▷ measure bribe by gap between marginal product of capital and gross return to investors.
- Most fruitful comparisons may be across countries.

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#### **Questions:**

- 1. Observable implications BG look at net worth or credit spreads; what is the equivalent here? The net worth of the financial sector?
- 2. Welfare example where workers willing to pay taxes to subsidize financial sector depends on concave r(I) funciton. r(I) just as easily convex: Cobb-Douglas production, full deprecitation, fixed labor supply now workers want cycles application of insight of Walter Oi that marginal revenue products of a fixed factor are convex.
- 3. How close model? Where do banker's come from? Assumes elstic supply of bankers, but bankers get bonus' and everyone can't be a banker. What

happens when supply of banker's inelastic or reward pinned down by cost of education. Effect of curvature? lots of multiple equilibria. Which survive additional curvature in utility, production, etc.

- 4. Interpretation
  - Firms or individuals?
- 5. Positive or normative?

Questions:

1. where do bankers come from?

- 2. Welfare
  - investors do not care
  - bankers and workers depends on properties of I

Complements from the Chef

Look at menu

reason for recession – high r – is that expect such a boom in the future that investing more today will lower average r below X

Techer cohorts and government spending.

Blanchard Yaari

inada conditions

risk

smoothing motives from the production side of the economy – the consumption euler equation

**Overview** 

- Partial equilibrium model of investment cycles due to moral hazard
- Starting point: observation that long-term relationships and backloading of incentives efficient responses to moral hazard problems in dynamic settings.

▷ Introduces into problem

- Shows that optimal contract and optimal investment do very little to restrict the path of interest rates.
  - $\triangleright$  Pin down average over *n* periods.
  - ▷ Lower bound on level, upper bound on growth rate.

**Elements of simple model** 

- Risk neutrality
- Relationships of length n.
- $\bullet\,$  Outside option with return  $1-\rho$
- Return to sucessful project  $r(I_t)$
- $\bullet\,$  Well managed project suceeds with probability  $\alpha$

- Cost of project *E* (per unit)
- An amount *B*, the minimum payment (per unit) to the banker that promotes good behavior.

#### **E**xcess return to invetors

$$\sum_{s=0}^{n-1} \left(\frac{\alpha}{1+\rho}\right)^{s+1} h_s \left[r_{t+s+1} - E - \frac{1+\rho}{\alpha}\right] - \frac{\alpha^n b_n}{(1+\rho)^n}$$

Choose  $h_s$  to maintain incentive

$$h_s B = b_n \left(\frac{\alpha}{1+\rho}\right)^{n-(s+1)}$$

 $h_0 = 1$  pins down  $b_n$ 

$$b_n = B\left(\frac{1+\rho}{\alpha}\right)^{n-1}$$

it follows that

$$h_s = \left(\frac{1+\rho}{\alpha}\right)^s$$

so that the size of the resources managed by agent multiplied by  $\frac{1+\rho}{\alpha}$  after each sucess

## **Excess return to investors**

Substituting

$$\sum_{s=0}^{n-1} \frac{\alpha}{1+\rho} \left[ r_{t+s+1} - E - \frac{1+\rho}{\alpha} \right] - \frac{\alpha B}{1+\rho}$$

in equilibrium  $\boldsymbol{r}$  must satisfy

$$\sum_{s=0}^{n-1} \left[ r_{t+s+1} - E - \frac{1+\rho}{\alpha} \right] = B$$

# Model places restrictions on r process

• n period average constant

$$\frac{1}{n} \sum_{s=0}^{n-1} r_{t+s+1} = X = \frac{B}{n} + E + \frac{1+\rho}{\alpha}$$

 $\triangleright$  *n* period cylce

 $\bullet \ r$  not too low

$$r > E + \frac{1+\rho}{\alpha}$$

• r does not grow too fast

$$I_{t} = \sum_{a=0}^{n-1} J_{t-a} (1+\rho)^{a}$$
$$J_{t} = \frac{(1+\rho)I_{t-1} - I_{t}}{(1+\rho)^{n} - 1}$$
$$I_{t} \leq (1+\rho)I_{t-1}$$

Model first step along a path. Lots of work to be done, before can quantify it. Like original Bernanke Gertler model